

# Messages about Collaboration meeting:

## **Adam:**

Due to the fact that this week is an official holiday in Russia, I propose to move the MPD Convenors meeting from tomorrow (April 1st) to next Wednesday (April 8th).

In the meantime, please let me know if You have proposals for the presentations during the "Physics Discussions" session of the Collaboration Meeting. I hope that we can finalize the agenda for this session during the meeting next week.

## **Natalia:**

On behalf of the Organizing Committee I would like to invite you to register for the V-th Collaboration Meeting of the MPD Experiment at the NICA Facility which will be held as a videoconference on April 23-24, 2020. Details of the connection procedure will be announced in advance before the conference.

The registration is available at the [www-page](https://indico.jinr.ru/e/5mpd_meeting) of the meeting:

[https://indico.jinr.ru/e/5mpd\\_meeting](https://indico.jinr.ru/e/5mpd_meeting)



# Vth MPD Collaboration meeting

23-24 April 2020, JINR, Dubna



## Correlation femtoscopy and factorial moments

on behalf of PWG3 (Correlations and Fluctuations)  
Supported by the RFBR grant 18-02-40044



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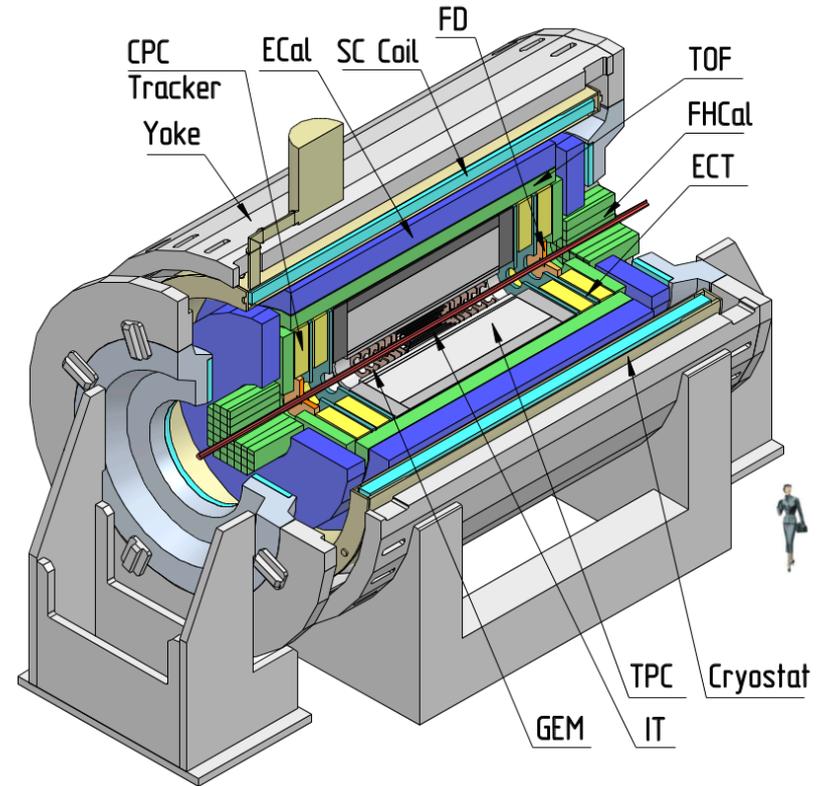
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# Outline

- Activities
- Femtoscopy & Motivation
- Hybrid vHLLE+UrQMD model
- Comparison with STAR BES
  - pions
  - first results with kaons
- First tests with reconstructed data
- Factorial Moments
- Other activities
- Plans for 20202
- Conclusion



# Activities within RFBR grant 18-02-40044 (2019)

## Aim of the project:

**Study of collective effects and dynamics of quark-hadron phase transitions via femtoscopic correlations of hadrons and factorial moments of particle multiplicity at NICA energies**

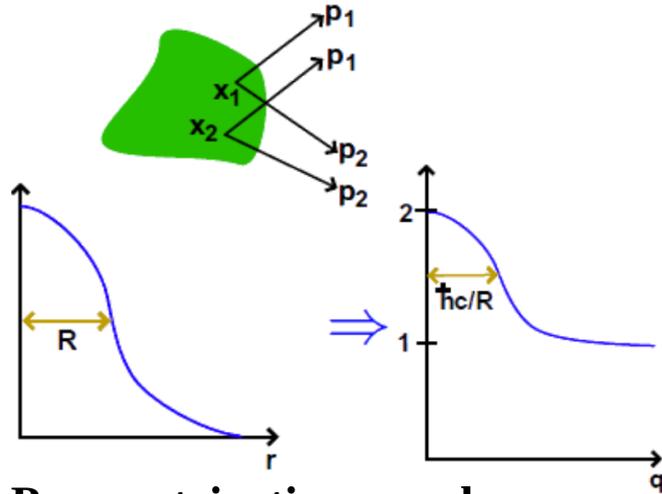
## Goals:

- Development of the data analysis methods and software that will be integrated in the Multi-Purpose Detector (MPD) software environment
- Analysis of the simulated with different event generators (in particular, UrQMD and vHLLE) Au+Au collisions at NICA energies
- Study the dependence of femtoscopic radii and scaled factorial moments of particle multiplicity on the initial conditions and properties of nuclear matter equation of state

## 2019:

- Simulation of Au+Au collisions with UrQMD and vHLLE+UrQMD models for different collision energies (**done**)
- Software development for: (**done**)
  - femtoscopic analyses
  - factorial moments of multiplicity distributions
  - other activities
- Femtoscopic analysis (at one collision energy) and extraction of source functions for pions and kaons for models with different Equation of State (EoS): first-order phase transition (1PT), crossover (XPT), no phase transition. (**done**)
- Investigation of the detector effects (track-merging and track-splitting in TPC) on femtoscopic measurements (**done**)

# Femtoscscopy



## Correlation femtoscopy :

Measurement of space-time characteristics  $\mathbf{R}$ ,  $\mathbf{ct}$  of particle production using particle correlations due to the effects of quantum statistics ( QS ) and final state interactions ( FSI )

## Two-particle correlation function:

theory: 
$$C(q) = \frac{N_2(p_1, p_2)}{N_1(p_1) \cdot N_2(p_1)}, C(\infty) = 1$$

experiment: 
$$C(q) = \frac{S(q)}{B(q)}, q = p_1 - p_2$$

$S(q)$  – distribution of pair momentum difference from same event  
 $B(q)$  – reference distribution built by mixing different events

### Parametrizations used:

1D CF: 
$$C(q_{inv}) = 1 + \lambda e^{-R^2 q_{inv}^2}$$

$R$  – Gaussian radius in PRF,

$\lambda$  – correlation strength parameter

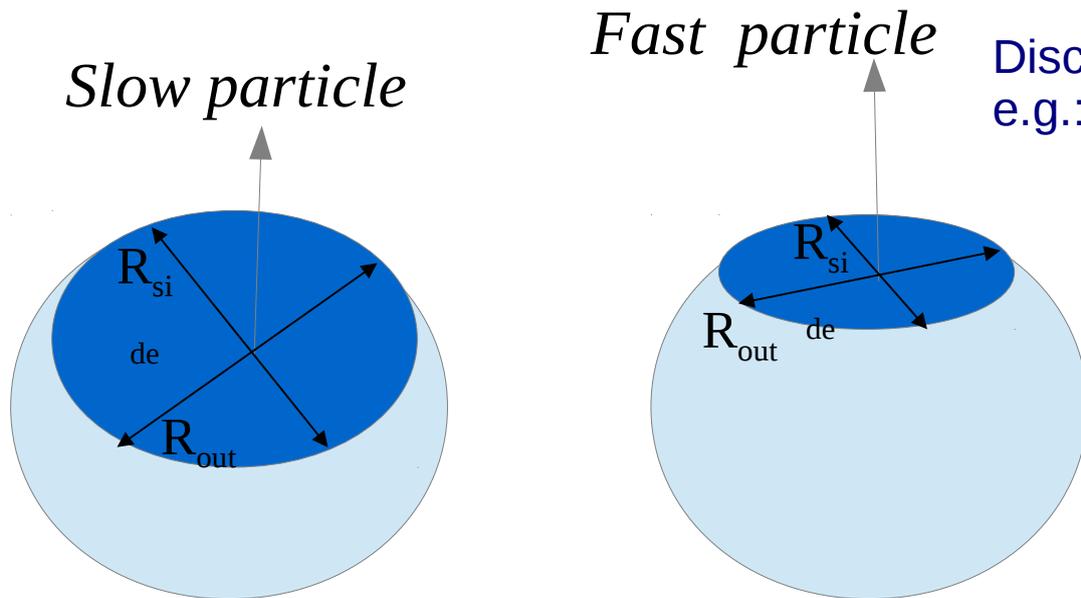
3D CF: 
$$C(q_{out}, q_{side}, q_{long}) = 1 + \lambda e^{-R_{out}^2 q_{out}^2 - R_{side}^2 q_{side}^2 - R_{long}^2 q_{long}^2}$$

$R$  and  $q$  are in Longitudinally Co-Moving Frame (LCMS)

long || beam; out || transverse pair velocity  $\mathbf{v}_T$ ; side normal to out, long

# Femtoscscopy with expanding source $\rightarrow m_T$ -dependence

- $\mathbf{x-p}$  correlations  $\rightarrow$  interference dominated by particles from nearby emitters.
- Interference probes only parts of the source at close momenta – **homogeneity regions**.
- Longitudinal and transverse expansion of the source  $\rightarrow$  significant reduction of the radii with increasing pair velocity, consequently with  $k_T$  (or  $m_T = (m^2 + k_T^2)^{1/2}$ )



Discussed in  
e.g.:

Kolehmainen, Gyulassy'86  
Makhlin-Sinyukov'87  
Pratt, Csörgö, Zimanyi'90

$$R_{\text{side}} \sim R / (1 + m_T \beta_T^2 / T)^{1/2}$$

$\beta_T$  collective transverse flow  
assuming a longitudinal boost  
invariant expansion

$$R_{\text{long}} = \tau (T/m_T)^{1/2}$$

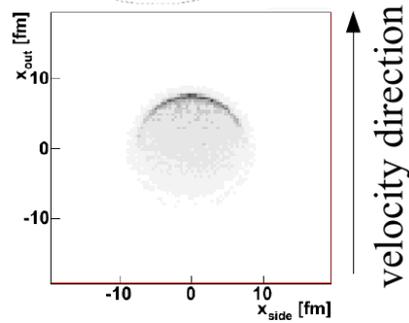
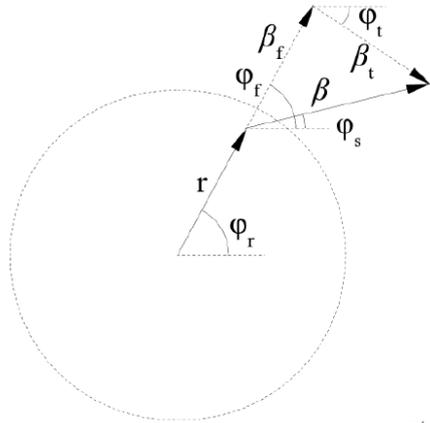
$$R_{\text{out}}^2 \sim R_{\text{side}}^2 + 1/2 (T/m_T)^2 \beta_T^2 \tau^2$$

# Femtoscscopy with expanding source

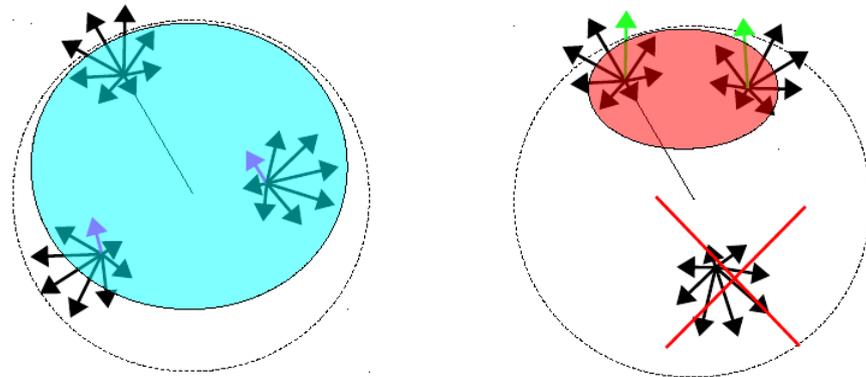
Interference probes only parts of the source at close momenta – **homogeneity regions**.

[Yu.M. Sinyukov, Nucl. Phys. A 566, 589 (1994);]

Figures and consideration from A. Kisiel Phys.Rev. C81 (2010) 064906

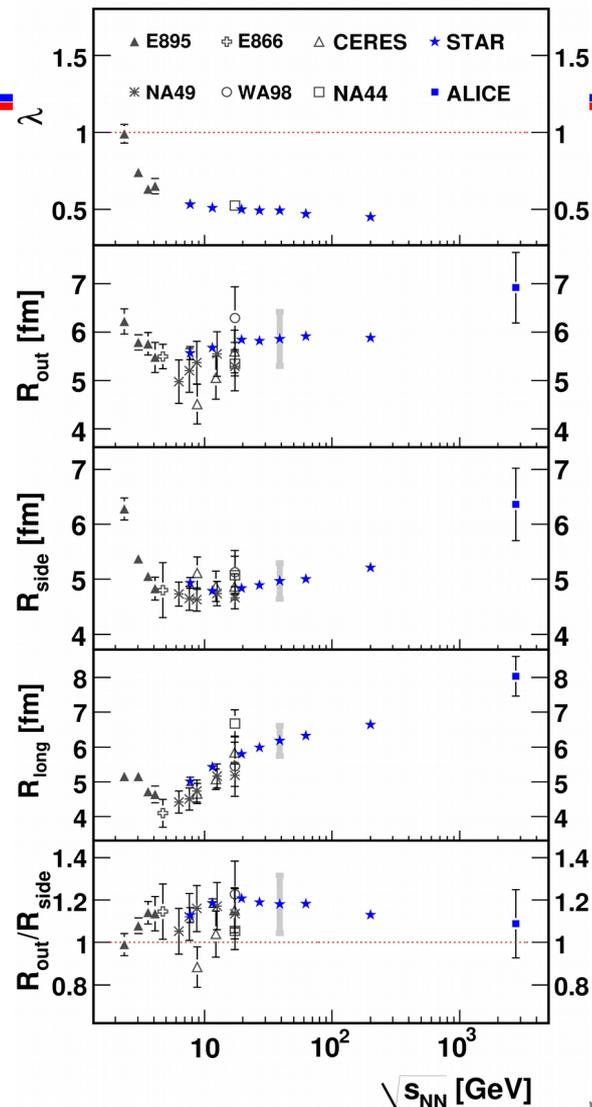


- A particle emitted from a medium will have a collective velocity  $\beta_f$  and a thermal (random) one  $\beta_t$
- As observed  $p_T$  grows, the region from where pairs with small relative momentum can be emitted gets smaller and shifted to the outside of the source



# Motivation

- **Femtoscopy allows one:**
  - To obtain spatial and temporal information on particle-emitting source at kinetic freeze-out
  - To study collision dynamics depending on EoS
- **RHIC Beam Energy Scan program (BES-I):**  
 $\sqrt{s_{NN}} = 7.7, 11.5, 19.6, 27, 39$  GeV
  - The search for the onset of a first-order phase transition in Au + Au collisions
  - Measured pion and kaon femtoscopic parameters:
    - $m_T$ -dependence of radii,
    - flow-induced  $x - p$  correlations
- NICA energy range:  $\sqrt{s_{NN}} = 4 - 11$  GeV  
measurements with great accuracy



# Femtoscropy with vHLE+UrQMD

Iu. Karpenko, P. Huovinen, H. Petersen, M. Bleicher, Phys.Rev. C 91, 064901 (2015)

Pre-thermal phase

UrQMD

Parameters  $\tau_0$ ,  $R_{\perp}$ ,  $R_{\eta}$  and  $\eta/s$  adjusted using basic observables in the RHIC BES-I region.

| $\sqrt{s_{NN}}$ [GeV] | $\tau_0$ [fm/c] | $R_{\perp}$ [fm] | $R_{\eta}$ [fm] | $\eta/s$ |
|-----------------------|-----------------|------------------|-----------------|----------|
| 7.7                   | 3.2             | 1.4              | 0.5             | 0.2      |
| 8.8 (SPS)             | 2.83            | 1.4              | 0.5             | 0.2      |
| 11.5                  | 2.1             | 1.4              | 0.5             | 0.2      |
| 17.3 (SPS)            | 1.42            | 1.4              | 0.5             | 0.15     |
| 19.6                  | 1.22            | 1.4              | 0.5             | 0.15     |
| 27                    | 1.0             | 1.2              | 0.5             | 0.12     |
| 39                    | 0.9             | 1.0              | 0.7             | 0.08     |
| 62.4                  | 0.7             | 1.0              | 0.7             | 0.08     |
| 200                   | 0.4             | 1.0              | 1.0             | 0.08     |

Model tuned by matching with existing experimental data from SPS and BES-I RHIC

Hydrodynamic phase

vHLE

(3+1)-D viscous hydrodynamics

EoS to be used in the model

- Chiral EoS — crossover transition  
J. Steinheimer et al., J. Phys. G 38, 035001 (2011)
- Hadron Gas + Bag Model  
1st-order phase transition  
P. F. Kolb et al., Phys.Rev. C 62, 054909 (2000)

Hydrodynamic phase lasts longer with 1PT, especially at lower energies but cascade smears this difference.

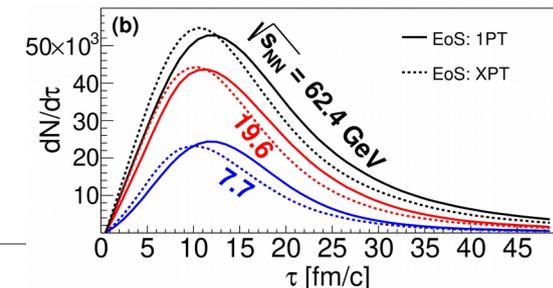
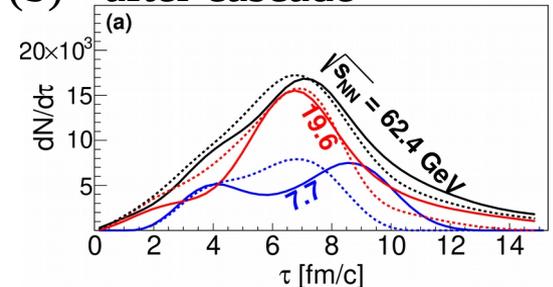
Hadronic cascade

UrQMD

Pion emission time

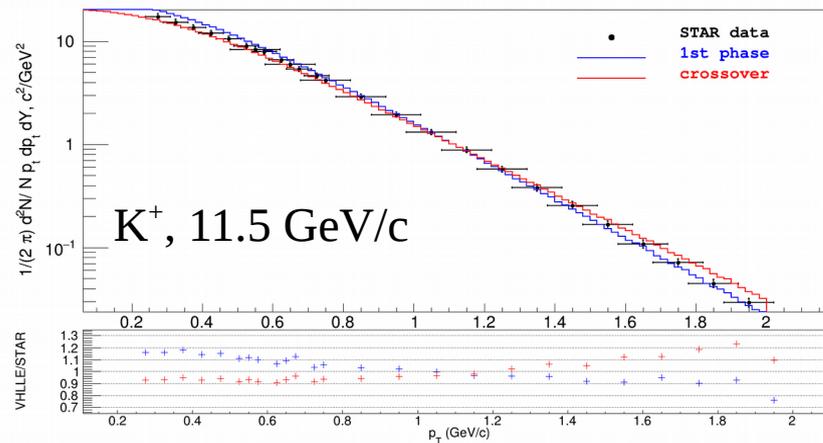
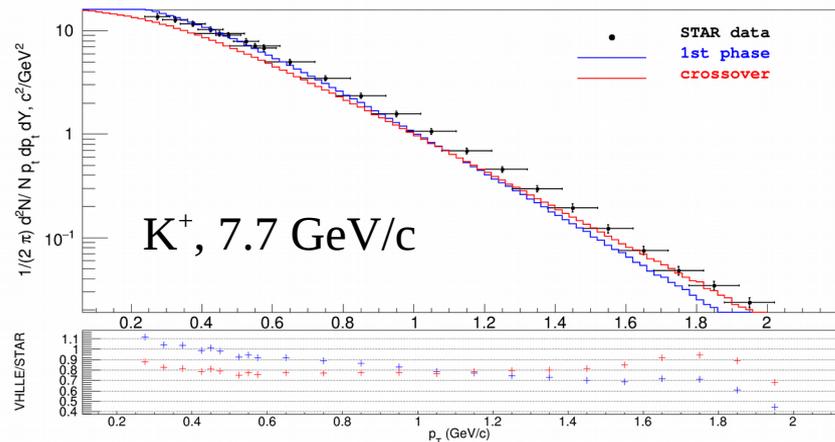
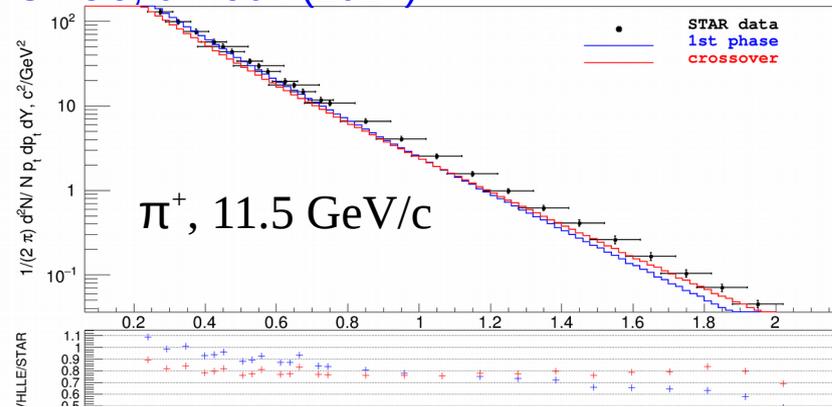
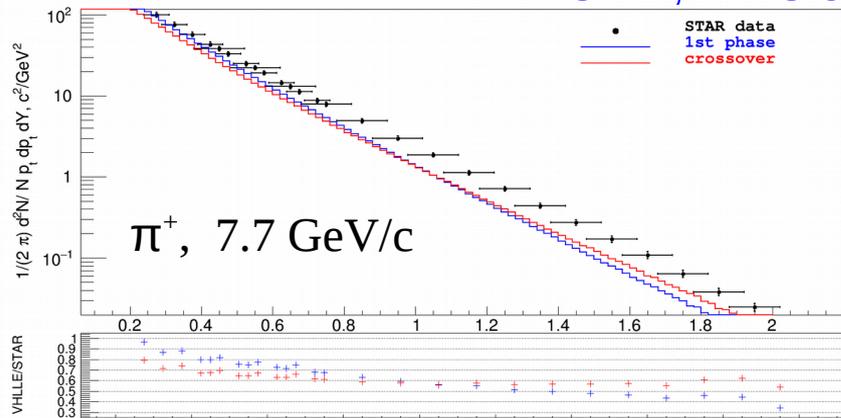
(a) - after hydrodynamic phase

(b) - after cascade



# $p_T$ -spectra of $\pi$ and K with $\nu$ HLEE+UrQMD

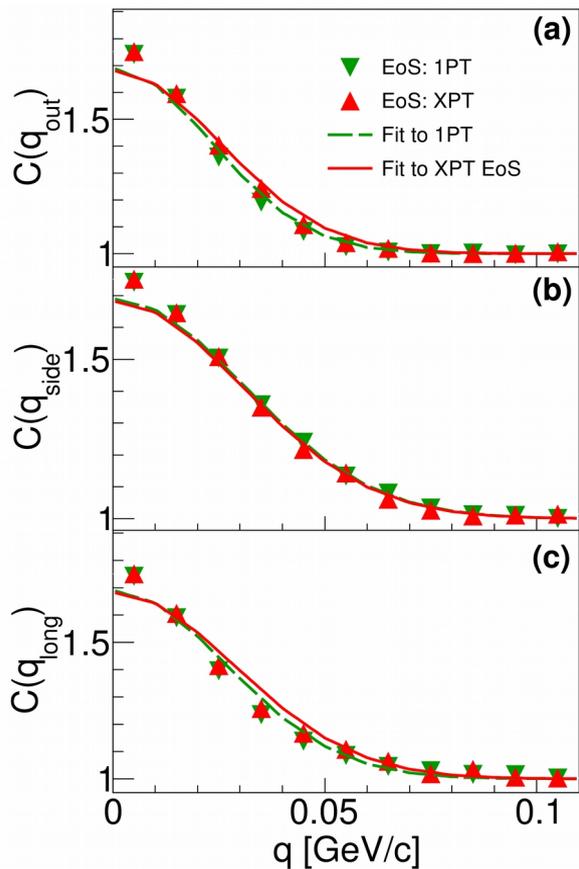
STAR, PHYSICAL REVIEW C 96, 044904 (2017)



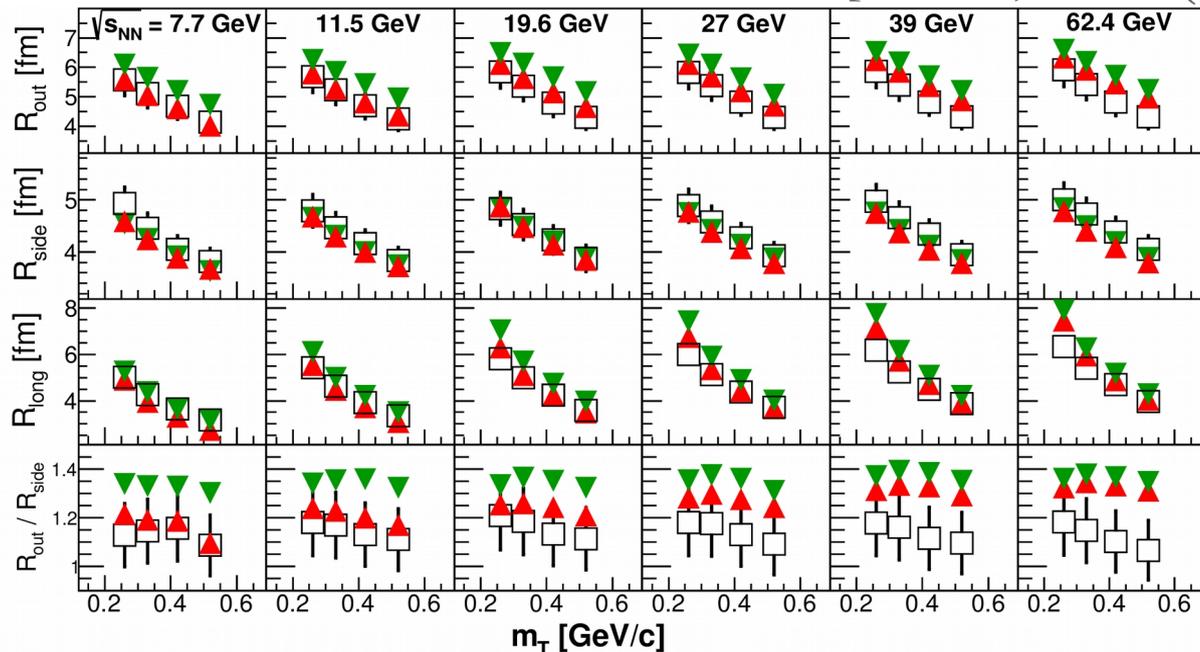
$\nu$ HLEE+UrQMD model with both EoS describe reasonably (<20%)  $p_T$ -spectra of pions and kaons at  $p_T < 1$  GeV/c

# 3D Pion radii versus $m_T$ with vHLLE+UrQMD

## Model CF



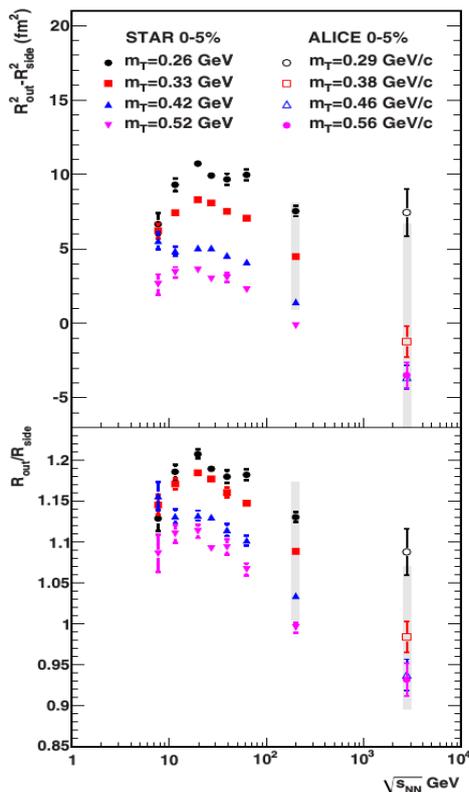
## Comparison of extracted radii with the STAR data [PRC 96, 024911(2017)]



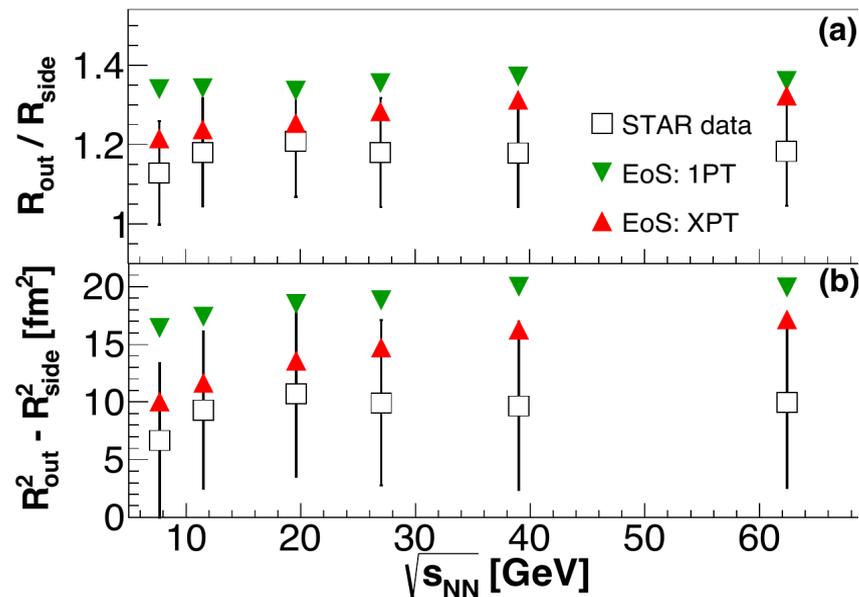
- Femtoscopic radii are sensitive to the type of the phase transition
- **Crossover EoS** does better job at lowest collision energies.
- $R_{out}$  (XPT) at high energies and  $R_{out}$  (1PT) at all energies are slightly overestimated
- $R_{out, long}$  (1PT)  $>$   $R_{out, long}$  (XPT) by value of  $\sim 1-2$  fm.

# $R_{\text{out}}/R_{\text{side}}$ with vHLLE + UrQMD model

**Exp. data:**  $R_{\text{out}}/R_{\text{side}}$  and  $R_{\text{out}}^2 - R_{\text{side}}^2$  as a function of  $\sqrt{s_{\text{NN}}}$  at a fixed  $m_{\text{T}}$  demonstrate a wide maximum near  $\sqrt{s_{\text{NN}}} \approx 20$  GeV

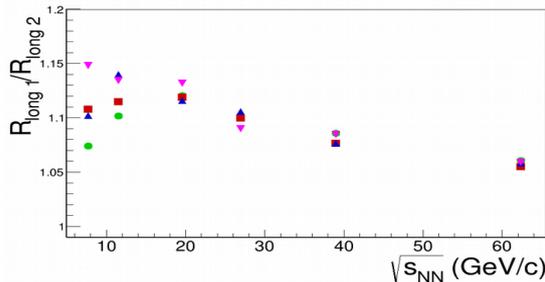
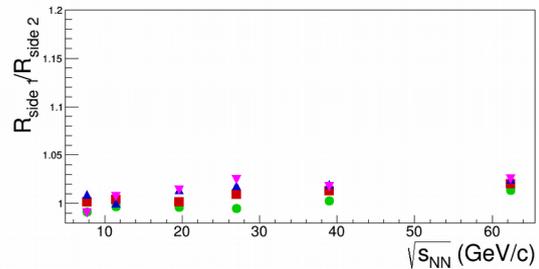
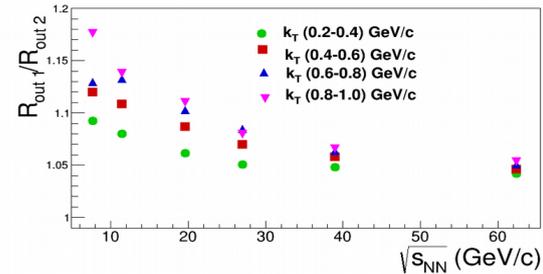


## Present vHLLE+UrQMD calculations:



- $R_{\text{out}}/R_{\text{side}}$  (**XPT**) agrees with almost all STAR data points within rather large systematic errors, while  $R_{\text{out}}/R_{\text{side}}$  (**1PT**) overestimates the data.
- **XPT** – a monotonic increase in both quantities

# Ratio of $R_{\text{out,side,long}}(1\text{PT})/R_{\text{out,side,long}}(\text{XPT})$ vs. $\sqrt{s_{\text{NN}}}$

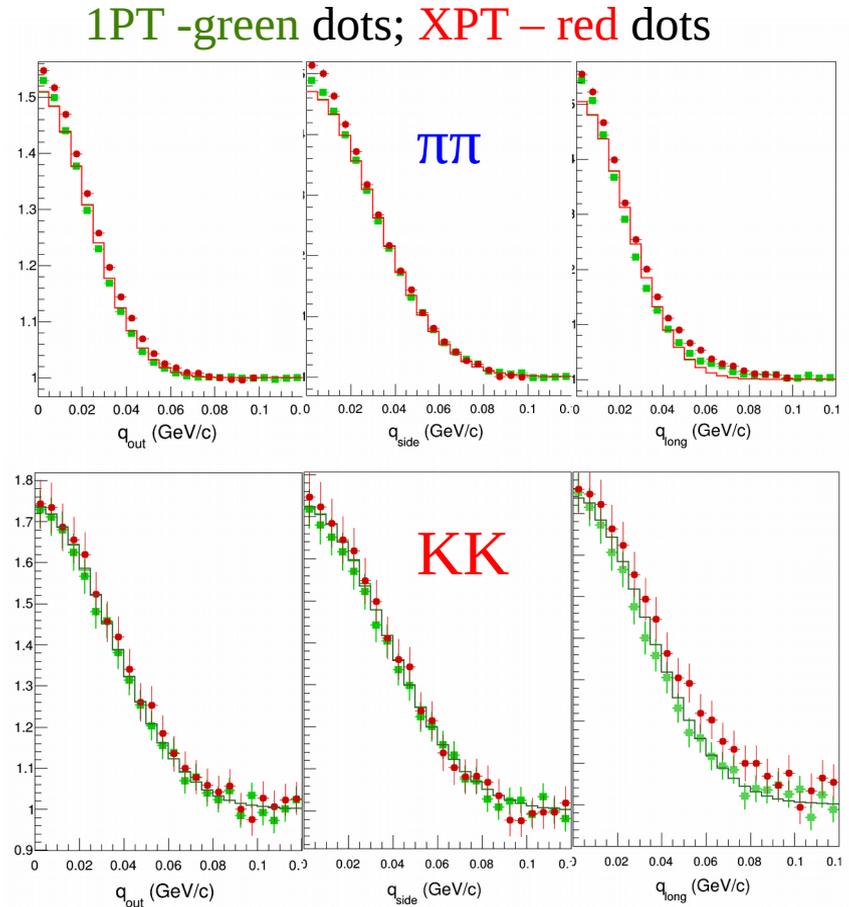


- Pion  $k_T$  divided into 4 bins
- $R_{\text{side}}$  ratio practically coincide for both scenarios
- $R_{\text{out}}$  and  $R_{\text{long}}$  ratios for 1PT EoS are greater than for XPT EoS and demonstrating a strong  $k_T$ -dependence at low energy
- The difference comes from a weaker transverse flow developed in the fluid phase with 1PT EoS as compared to XPT EoS and its longer lifetime in 1PT EoS

# Kaon correlation functions with vHLLE+UrQMD (NEW!)

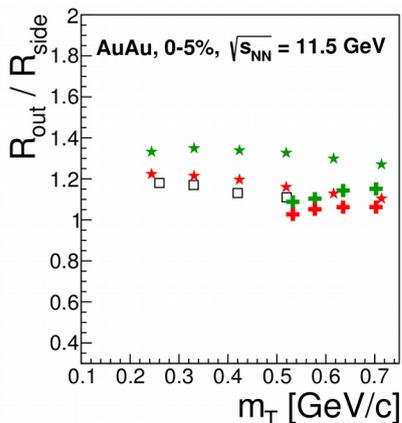
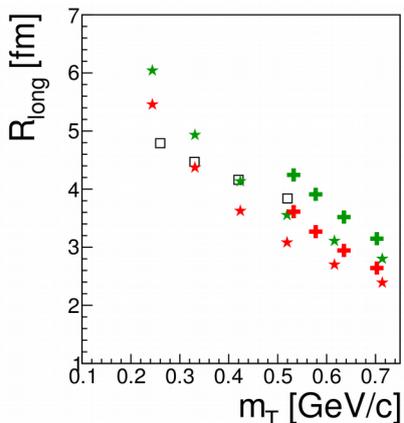
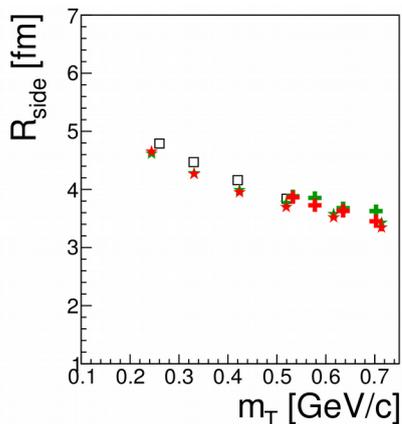
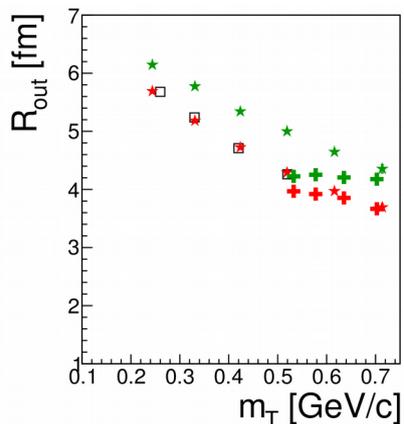
## Analysis:

- Au+Au,  $\sqrt{s}_{NN} = 11.5$  GeV
- $N_{\text{events}} \approx 4 \cdot 10^5$
- Standard 3D Gaussian fit used
- Our, side, long projections
  
- Projections of 3D kaon correlation functions on out-side-long directions are more Gaussian
  
- **XPT** CF projections on long direction are visibly wider than **1PT** especially for kaons



# Radii $\pi$ and K vs. $m_T$ with $\nu$ HLE+UrQMD

1PT -green dots; XPT - red dots



- Au+Au,  $\sqrt{s_{NN}} = 11.5$  GeV
- As well as for  $\pi$ , kaon out and long radii greater for 1PT than for XPT
- Approximate  $m_T$ -scaling for pions and kaons observed only for “side” radii
- $R_{out}$  almost flat for 1PT
- $R_{long}(KK)$  is greater than  $R_{long}(\pi\pi)$  kaons on average emitted later than pions
- $R_{out}/R_{side}(KK)$  for kaons is less than for pions
- Approximately the same result is for Au+Au  $\sqrt{s_{NN}} = 7.7$  GeV
  
- It is important to measure both kaons and pions

# Factorial moments

Proposed by A. Bialas and R. Peschanski (Nucl. Phys. B 273 (1986) 703) to study the dependence of the normalized factorial moments of the rapidity distribution on the size of the resolution

The scaled factorial moments are defined:

$$F_i = M^{i-1} \cdot \left\langle \frac{\sum_{j=1}^M k_j \cdot (k_j - 1) \cdot \dots \cdot (k_j - i + 1)}{N \cdot (N - 1) \cdot \dots \cdot (N - i + 1)} \right\rangle$$

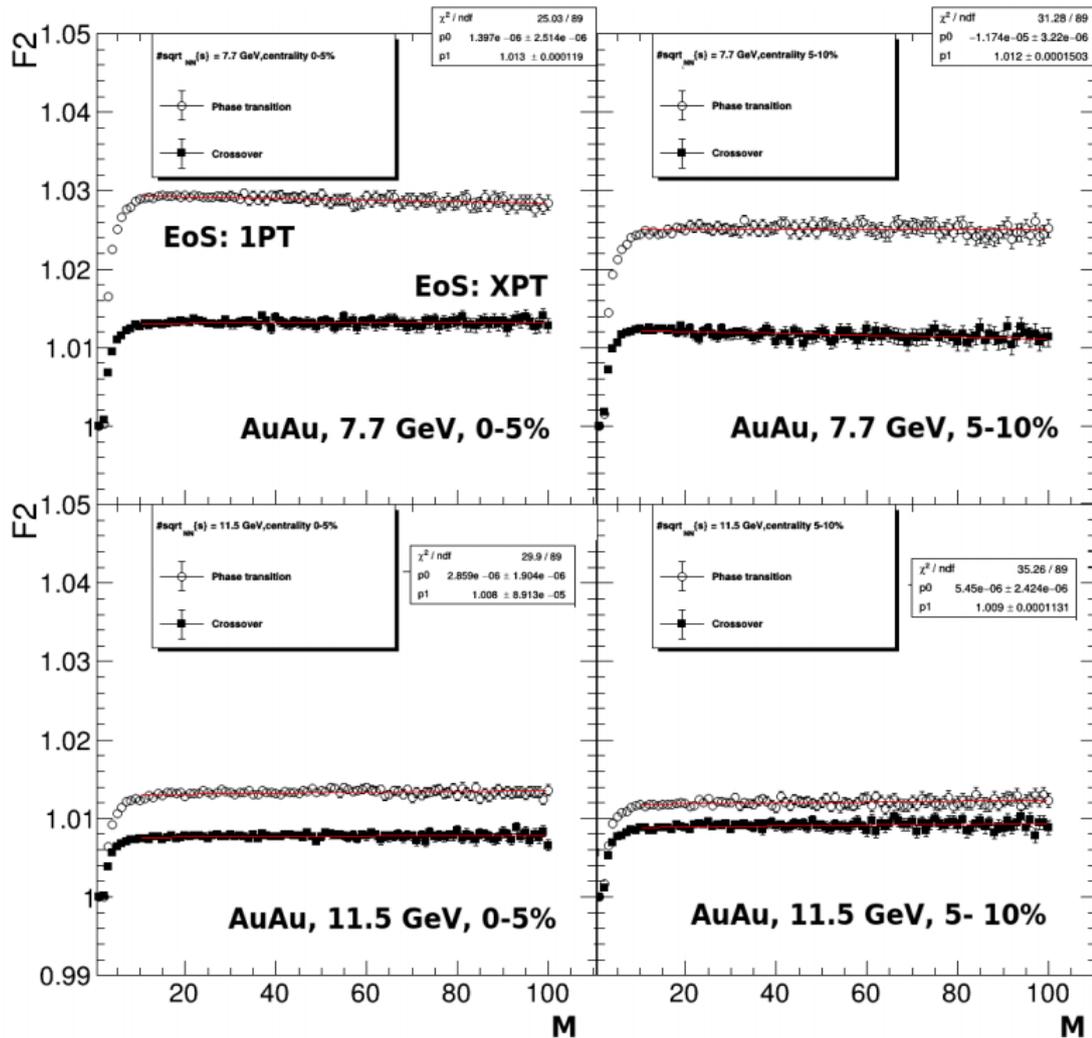
where brackets  $\langle \rangle$  denote averaging over a sample of a selected class of events.

$N = k_1 + \dots + k_M$  is a total number of particles, and  $M$  is number of intervals in rapidity window.

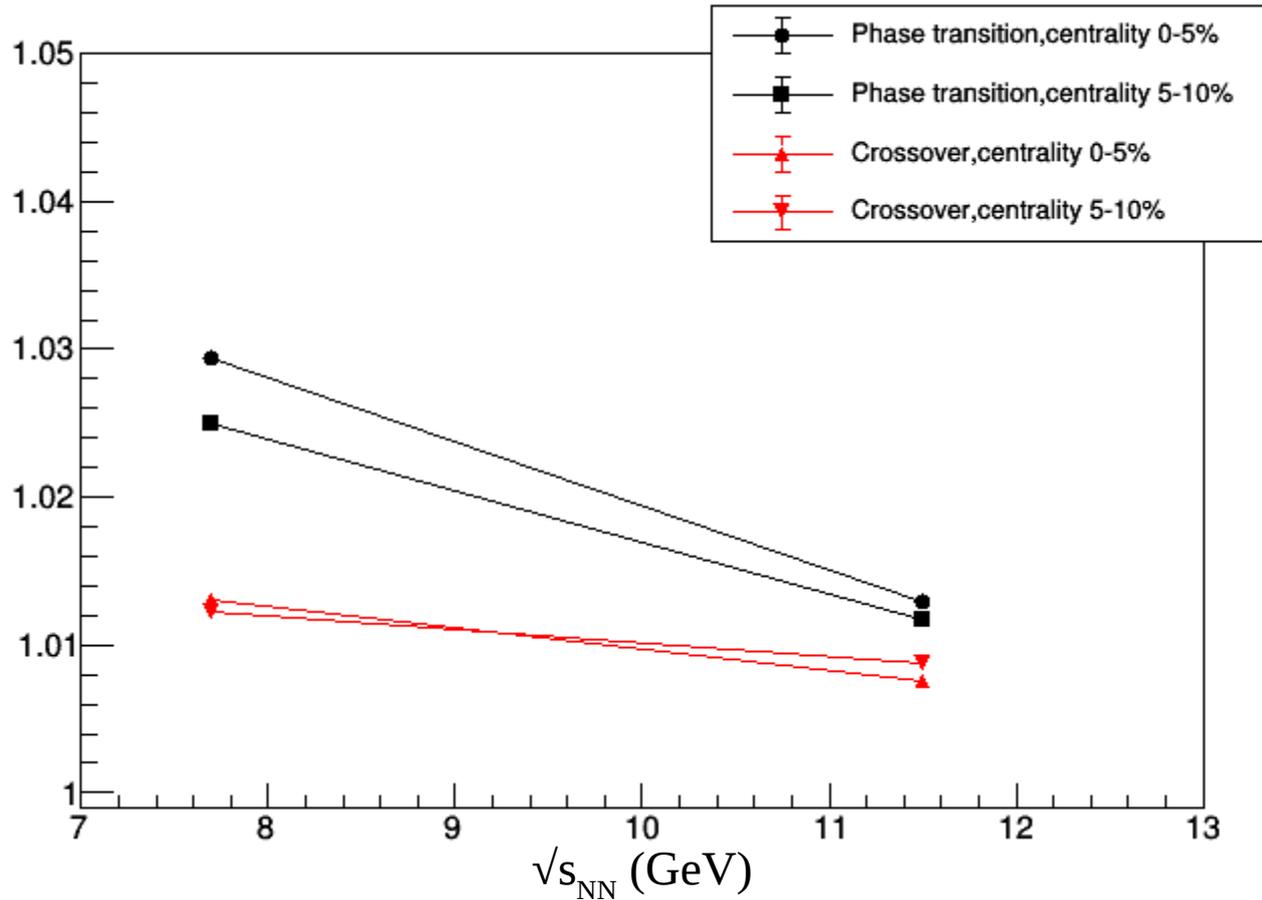
- Factorial moments do not depend on  $M$  in case of statistical fluctuation of rapidity distribution
- And  $F$  depend on  $M$  if fluctuation due to physical reason.

# Factorial moments with vHLLE+UrQMD

- $F_2$  as a function  $M$  for  $|y| < 0.5$
- Fit  $F_2$  by the first order polynomial:  $a + bM$   
 $b$  is of the order of  $10^{-6}$
- $F_2$  maximum is determined from fit



# Energy dependence of F2 maximum



- Plot the F2 max as a function of energy.
- F2 energy dependence is expected for Crossover and 1<sup>st</sup> order phase transition

# 2020 plans

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- Simulation of ion-ion collisions with different models and different EoS for  $\sqrt{s_{NN}}=4-11\text{GeV}$  energies to be continued
  - 3d CF analysis of  $\pi\pi$  and  $KK$
  - $m_T$  dependence within MPD detector range
  - Factorial moment study
- New MpdFemto package
  - Test within MpdRoot
  - Two Track Cut tests (merging, splitting)
  - Finite Momentum Resolution tests
- New miniDST format
  - Compact reconstructed and generated information (ten times less than DST)
  - Reaction, track quality, TOF, Ecal and FHCAL (first stage of MPD detector)
  - MiniDST created on-the-fly
- Software for factorial moment study will be developed

# Conclusions

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- Study of collective effects and dynamics of quark-hadron phase transitions via femtoscopic correlations of hadrons and factorial moments of particle multiplicity at NICA energies was performed
- First results look promising and this study is planned to be continued.
- Development of the data analysis methods and software integrated in the Multi-Purpose Detector (MPD) software environment was performed and will be continued
- Results were presented at WPCF, QFTHEP and NICA Days conferences
- Proceeding were published

*Thank you for attention!*

# Title

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# Title

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