



The XX International Baldin Seminar on High Energy Physics Problems "Relativistic Nuclear Physics and Quantum Chromodynamics", organized by the Joint Institute for Nuclear Research will be held October 4-9, 2010 in Dubna, Russia.



# Femtoscscopy application of the new EPOS model to the STAR and ALICE experiment

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- Motivation of the femtoscopy study with the Epos model
- Technical details of the Epos Femto package
- First results from Epos Femto package and comparison with STAR data
- Comparison with ALICE data and Non-femtoscopic effects
- Conclusions



- EPOS is not a simple MC event generator, Epos is a physical event model which includes all stages of collision (init. conditions from flux tube, EbE procedure, 3+1 hydrodynamics, realistic EoS, complete resonance table, hardonic cascade)
- EPOS provides space-time coordinates of hadrons
- Possibility to study femtoscopy with EPOS
- EPOS is very wide energy range model  
(applicability: pp, pA, AA, a tens  $\text{GeV} < \sqrt{s} < \text{a few TeV}$ )

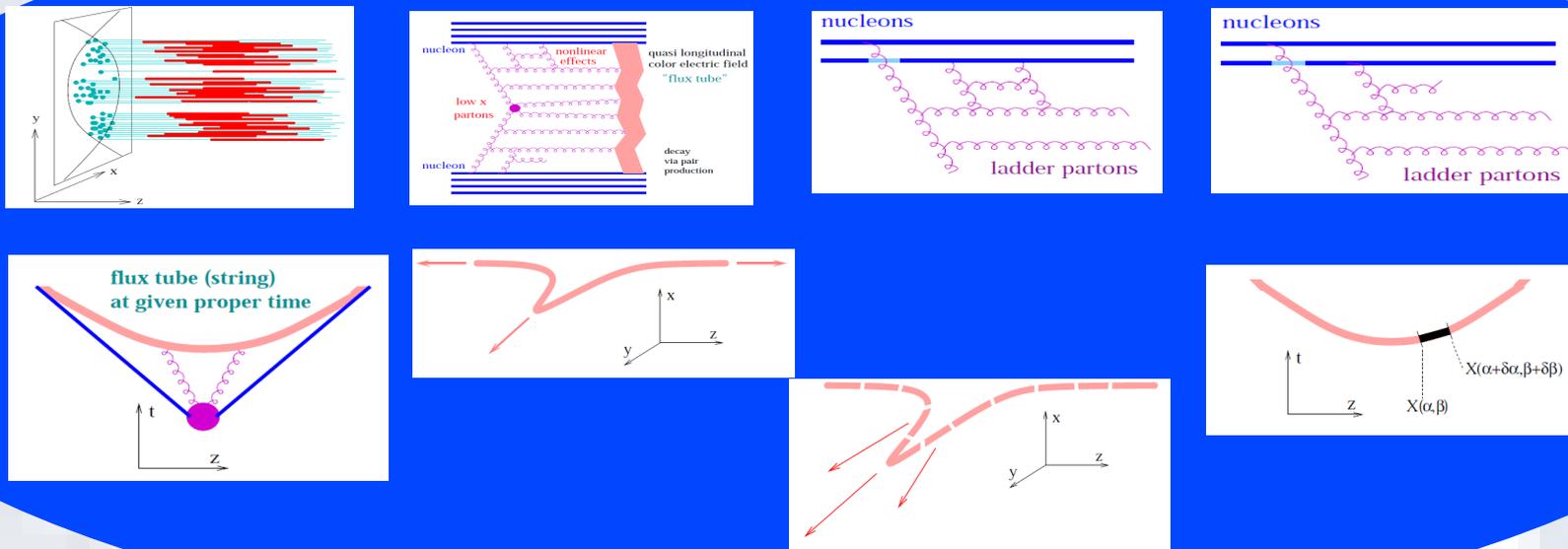


- Initial conditions obtained from flux tube approach (EPOS)
- Consider of the possibility to have a (moderate) initial collective transverse flow
- Event-by-event procedure
- Core-corona separation
- 3+1 hydrodynamic equation
- Realistic EoS
- Complete hadron resonance table
- Hadronic cascade after hadronization
- *All these above are applied to pp@LHC (completely new)!*

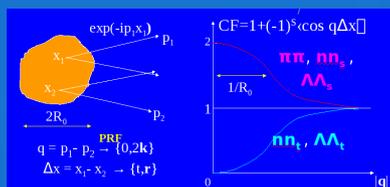
# Epos and Femto



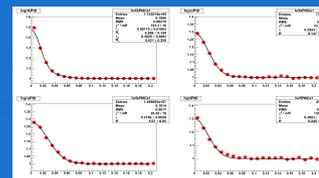
## EPOS code v.2 [arxiv.org/abs/1004.0805]



Connection via Epos Tree



**Femtoscscopy analysis**  
 1d, 3d,  $\pi\pi, KK, pp,$   
 $\pi\rho, \rho\Lambda, \dots$



**Radii,  $k_T$  ( $m_T$ ) dependence, centrality dependence, etc**

# Epos Femto Package features

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- Epos Femto package is a part of Epos2 code
- Femto could be used as a stand alone code (input **Epos Root Tree** events)
- Femto is a C++ code based on root framework
- The correlation function is calculated with event mixing technique:  $C = (dN_{\text{real}}/dQ)/(dN_{\text{mixed}}/dQ)$
- The correlation weight is provided by R.Lednicky code
- All pairs of particles which are in Lednicky's code could be studied in Epos Femto package
- It is possible to smear the momentum of the particle according to the detector response

# Go to the First results

K. Werner, Iu. Karpenko, T. Pierog,  
M. Bleicher, K. Mikhailov

<http://arxiv.org/abs/1004.0805>

<http://arxiv.org/abs/1010.0400>

# Correlation Function



Provides source function  $S(\mathbf{P}, \mathbf{r}')$  – probability of emitting a pair of hadrons with total momentum  $\mathbf{P}$  and relative distance  $\mathbf{r}'$  (from EPOS simulation).  
Under certain assumption,  $S$  is related to the measurable correlation function  $C(\mathbf{P}, \mathbf{q})$  as:

$$C(\mathbf{P}, \mathbf{q}) = \int d^3r' S(\mathbf{P}, \mathbf{r}') |\Psi(\mathbf{q}', \mathbf{r}')|^2$$

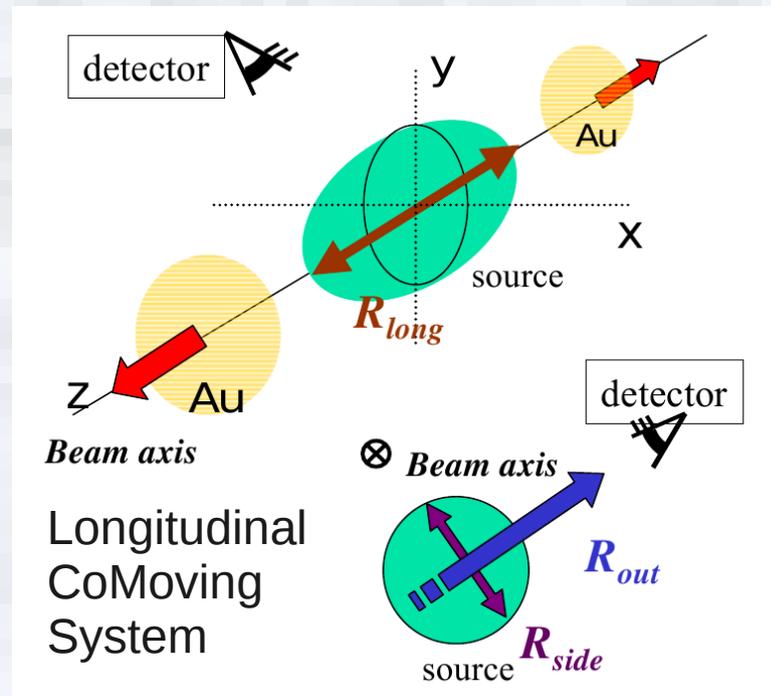
$q$ -relative momentum,  $\Psi$  outgoing two-particle wave function (Lednicky's code),  $q'$  and  $r'$  relative momentum and distance in pair CMS

CF parametrized by :

$$C(\mathbf{P}, \mathbf{q}) = 1 + \lambda \exp(-R_{out}^2 q_{out}^2 - R_{side}^2 q_{side}^2 - R_{long}^2 q_{long}^2)$$

Fit parameters  $\lambda$ ,  $R_{out}$ ,  $R_{side}$ , and  $R_{long}$  are determined for different centrality classes and for different  $m_T$ , with

$$m_T = \sqrt{k_T^2 + m^2}, \quad k_T = \frac{1}{2} (|\vec{p}_T(\text{hadron 1}) + \vec{p}_T(\text{hadron 2})|).$$



# Simulation: software and input



- EPOS 2, model details in <http://arxiv.org/abs/1004.0805>
- Compare with STAR HBT  $\pi\pi$  in AuAu collisions at  $\sqrt{s}=200$  GeV  
[PHYSICAL REVIEW C 71, 044906 (2005)]
- Analysis of Epos events
  - ~0.5 M events of AuAu collisions at 200 GeV ,
  - 5 **centrality** regions: 0–5%, 5–10%, 10–20%, 20–30%, 30–50%, and 50–80%
- **$k_T$**  regions: 150-250, 250-350, 350-450, 450-600 MeV/c
- STAR acceptance:  $0.15 < P_T < 0.8$  GeV/c,  $|\eta| < 0.5$
- Only Q.S. weight for  $\pi^+\pi^+$  pairs
- Fit function (3d):
$$1 + \lambda \exp(-R_{\text{out}}^2 Q_{\text{out}}^2 - R_{\text{side}}^2 Q_{\text{side}}^2 - R_{\text{long}}^2 Q_{\text{long}}^2)$$

# Different Epos model scenarios

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**We will compare three scenarios:**

- 1.) The **full** scenario:  
flux tube+hydro+hadronic cascade
- 2.) The calculation **without hadronic cascade**:  
with final freeze out at 166 MeV
- 3.) The **fully thermal scenario**:  
hydrodynamical evolution till a late freeze-out  
at 130 MeV and no hadronic cascade afterwards

# Source functions

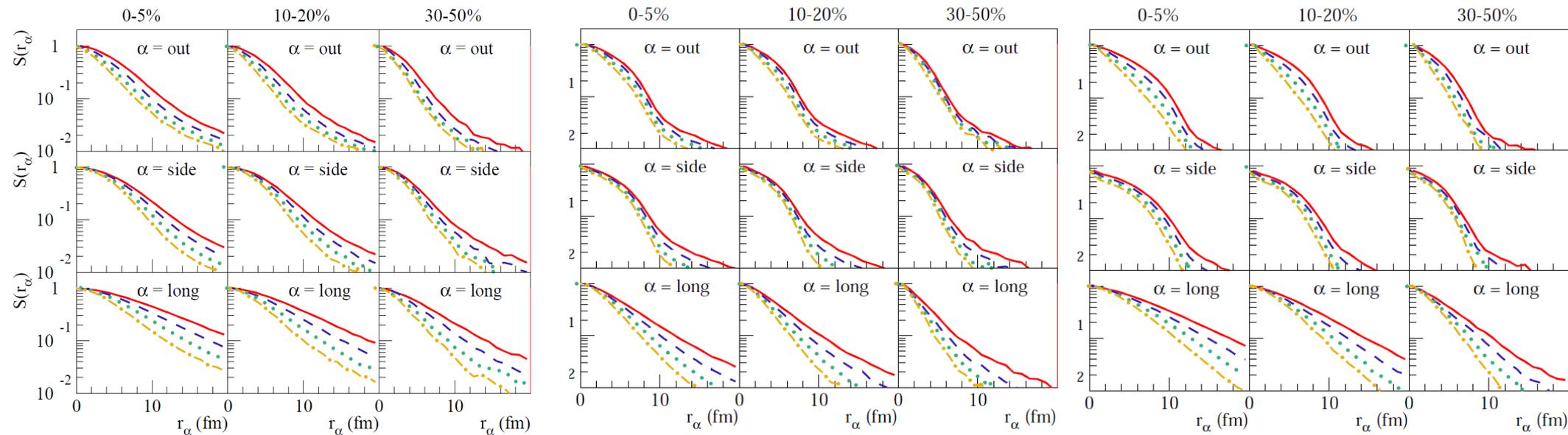


The source functions as obtained from our simulations, for three different centralities (0-5%, 10-20%, and 30-50%), representing the distribution of the space separation of the emission points of the pairs, in LCMS. **Full** curves – first  $k_T$  bin, **dashed** – second  $k_T$  bin, and so on. The curves get narrower with increasing  $k_T$  (decreasing radii). The curves get narrower with decreasing centrality (decrease of radii with decreasing centrality).

1. **full scenario**

2. **without hadronic cascade**

3. **fully thermal scenario**



The fitting procedure based on the hypothesis that the source function Gaussians and it does not sensitive to the non-Gaussian tails.

**One can expect similar results for scenario 1 and 3.**



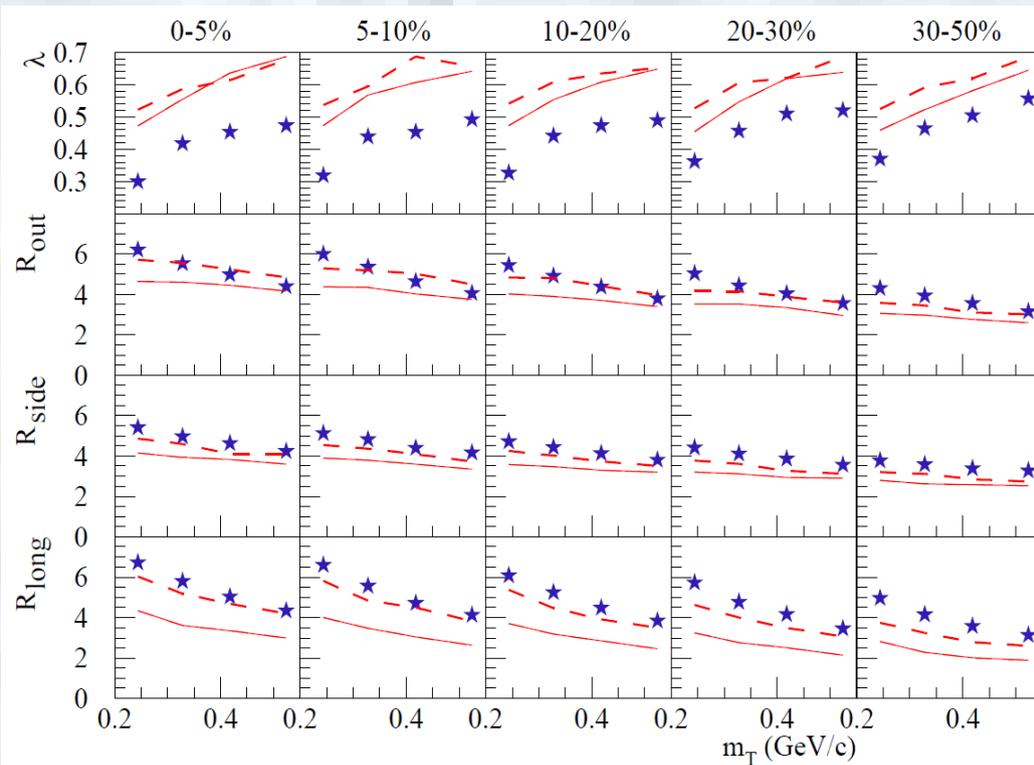
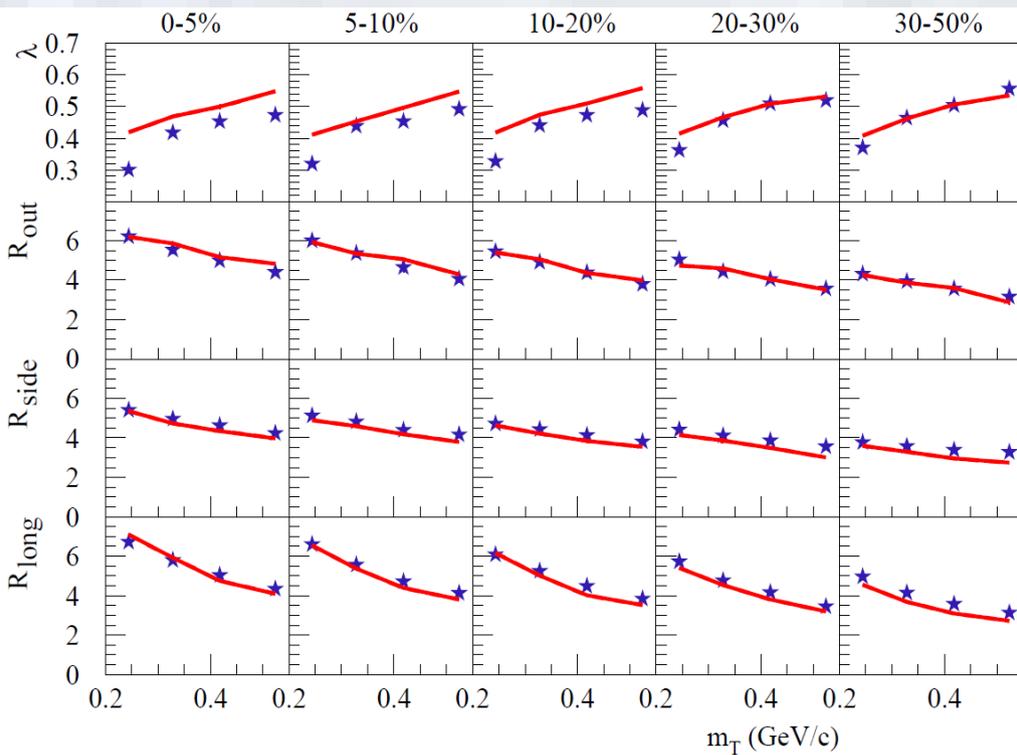
# Femtoscopic radii (different scenarios)

$R_{out}$ ,  $R_{side}$ , and  $R_{long}$  as a function of  $m_T$  for different centralities (0-5% most central, 5-10% most central, and so on). The star symbols are the data of STAR.

Left: **Thick full line** - full calculation, hydro&cascade (scenario 1).

Right: **Thin full line** - the calculations are done without hadronic cascade (scenario 2).

**Dashed lines** - with a hydrodynamic evolution through the hadronic phase with freeze-out at 130 MeV (scenario 3).



Scenario 1, scenario 3, and the data are similar.

It could be better to compare the shape of CF, not only radii

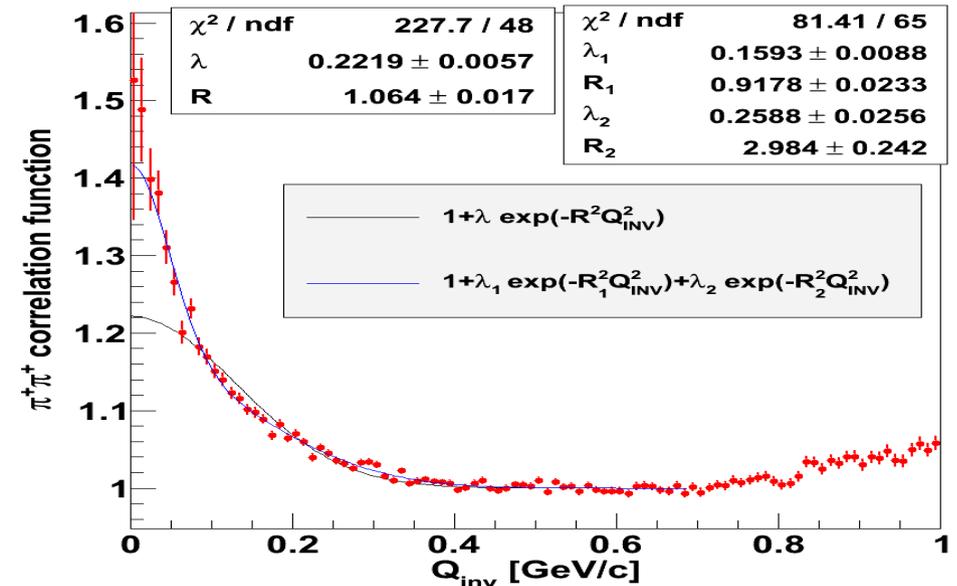
ALICE pp and Non-femtoscopic  
effects...

# Long range correlation

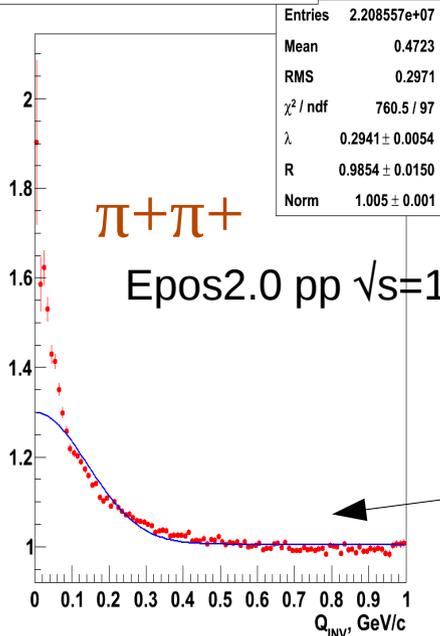


These correlations (so-called “long-range correlations” — **LRC**) arise mainly from momentum conservation for real events, which is not a requirement for mixed pairs. LRC cause a smooth increase of CF with  $q$ , which reflects the fact that due to momentum conservation the probability of two particles emitted in the same direction is smaller than that of two particles emitted in opposite directions. Empirically, LRC can be parametrized as  $R \propto \exp(b \cos \psi)$ , in which  $\psi$  is the angle between the two particles and  $b$  is a constant [A. V. Vlassov et al., *Phys. At. Nucl.* 58, 613 (1995)]. Practically, accounting for such a weak dependence of the correlation function on  $q$  is usually taken into account by introducing into data fit a factor  $(1 + \text{const } q^2)$

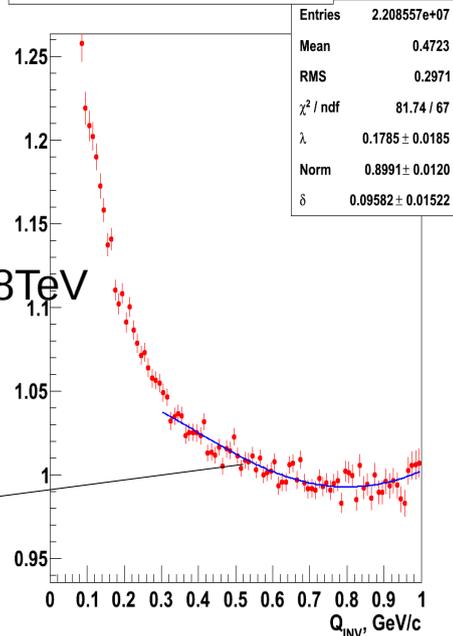
## Epos-1.90 pp $\sqrt{s}=900\text{GeV}$



## $\pi^+\pi^+$ correlation function (pp $\sqrt{s}=1.8\text{TeV}$ ) hqmAPI00



## $\pi^+\pi^+$ correlation function (pp $\sqrt{s}=1.8\text{TeV}$ ) hqmAPI00



## PYTHIA 7e5 pp events $\sqrt{s}=14\text{TeV}$



### $\pi^+\pi^+$ correlation function

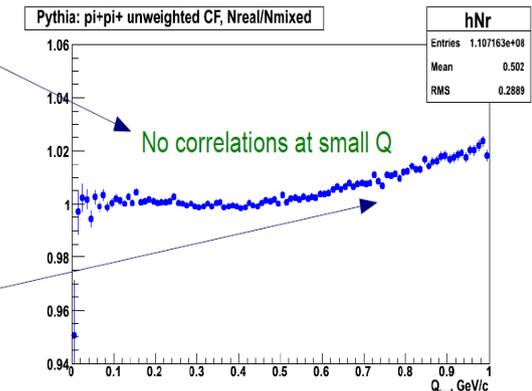
Cuts:

- $0.1 < P_T < 1.0\text{ GeV}/c$
- $-1. < \eta < +1.$

CF=Real/Mixed

Energy and Momentum Conservation-Induced Correlations:

Due to energy-momentum conservation probability of two particle emitted at same direction is smaller than in opposite direction

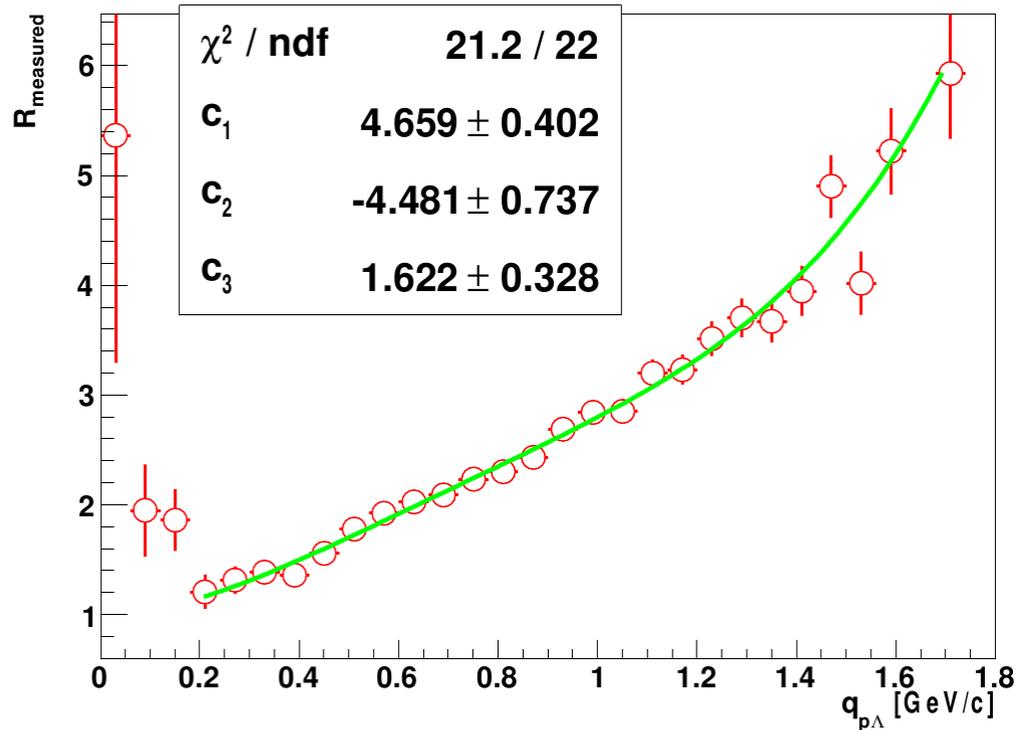




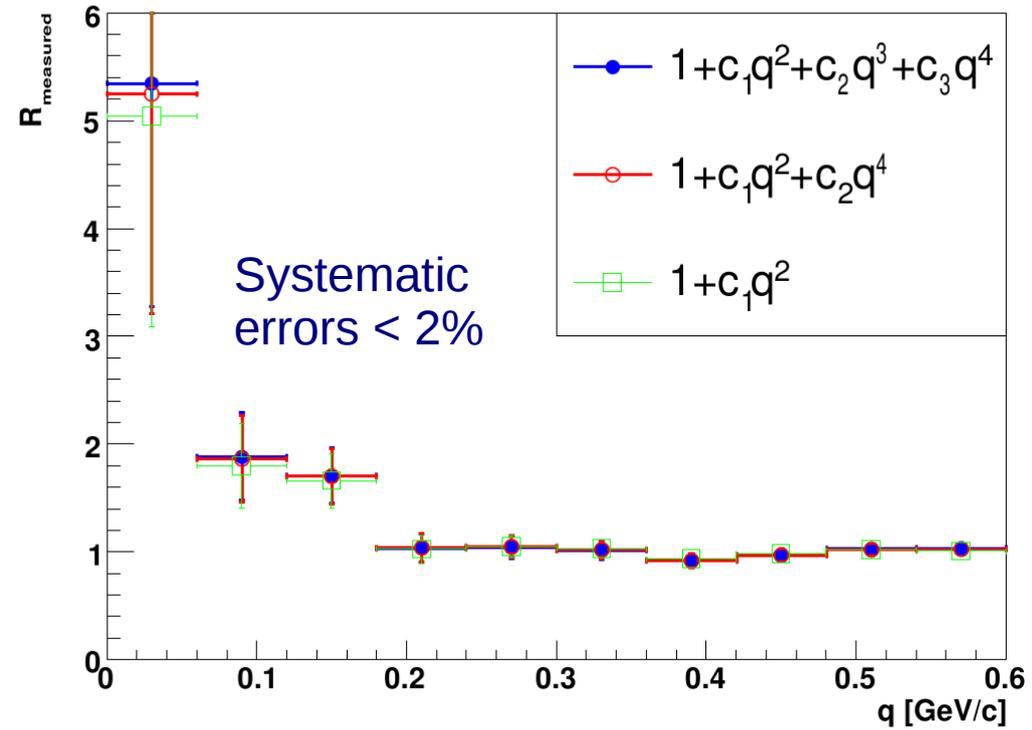
## Source-Size Measurements in the $e^3\text{He}(^4\text{He}) \rightarrow e'p\Lambda X$ Reaction

[Physics of Atomic Nuclei, 2009, Vol. 72, No. 4, pp. 668–674.]

$e^{3,4}\text{He} \rightarrow e'p\Lambda X$ , long-range correlation correction



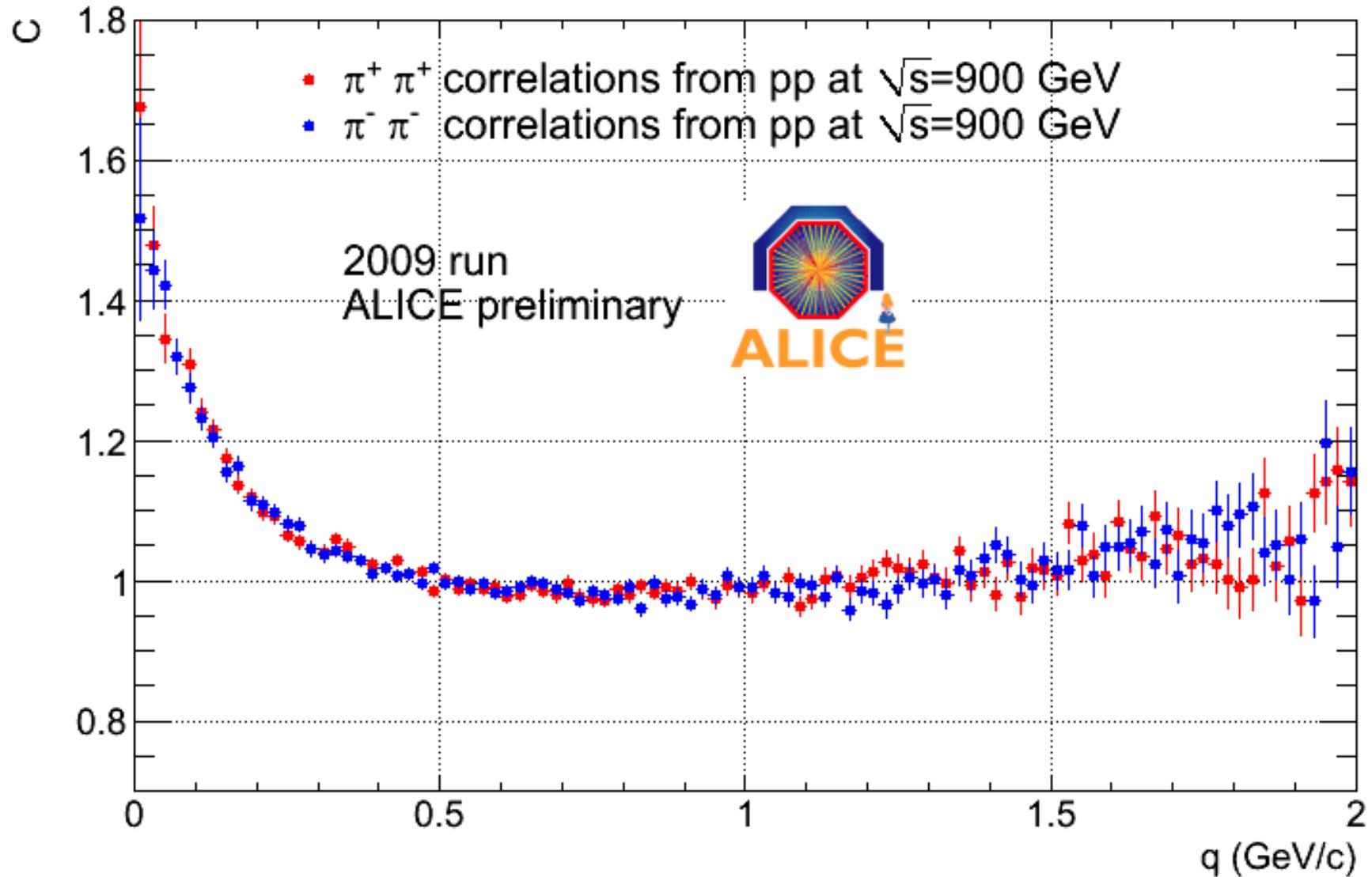
Comparison of LRC correction



# LRC in ALICE



Dariusz Miskowiec, Particle correlations in ALICE, Physics at the LHC, Hamburg, 10-Jun-2010



# Non-femtoscopic effects with EPOS



- $\pi\pi$  correlation in pp at  $\sqrt{s}=900\text{GeV}$  Epos 2.05 model calculation
- $k_T$  intervals [100,250],[250,400],[400-550],[550-700],[700-1000] MeV/c
- High multiplicity  $dN_{ch}/d\eta(0)=12.9$

- Full correlation function with mixing procedure (femto and non-femto):

$$CF = [dN_{real}/dq_{inv} * W(r,p)] / [dN_{mixed}/dq_{inv}]$$

- Pure femtoscopic correlation function (femto):

$CF = [dN_{real}/dq_{inv} * W(r,p)] / [dN_{real}/dq_{inv}]$ , where W is pure femtoscopic weight from Lednicky's code (QS only)

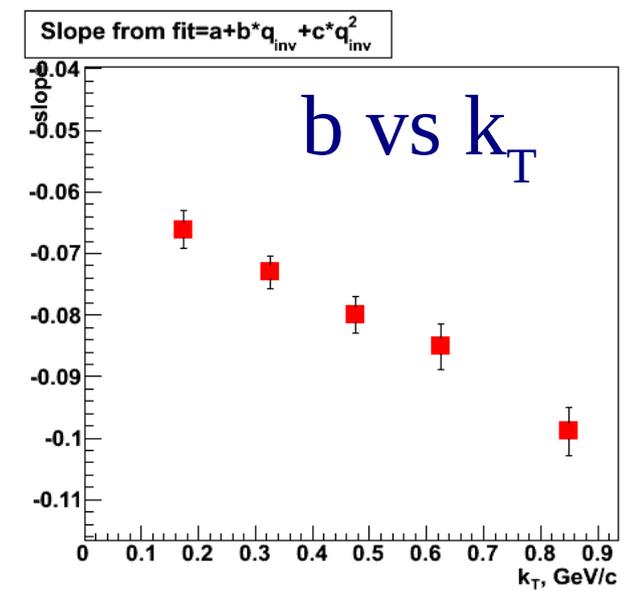
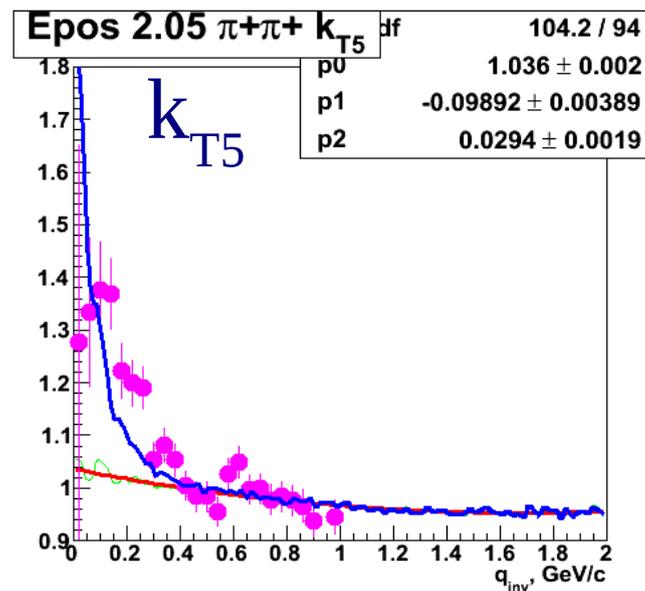
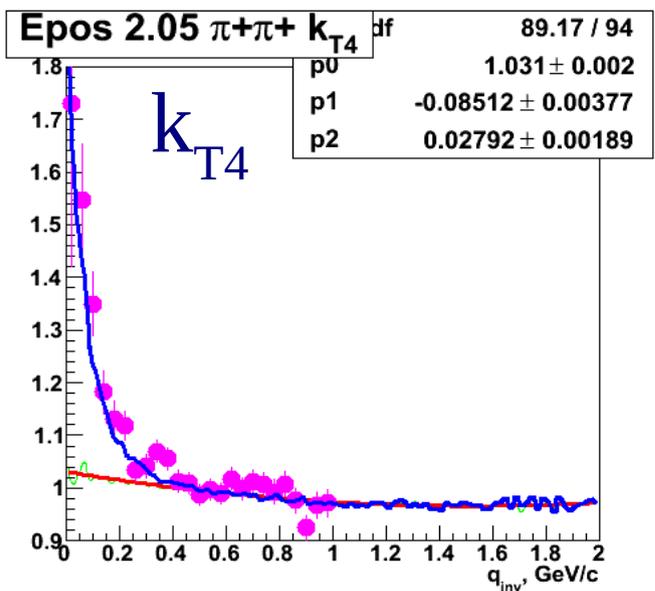
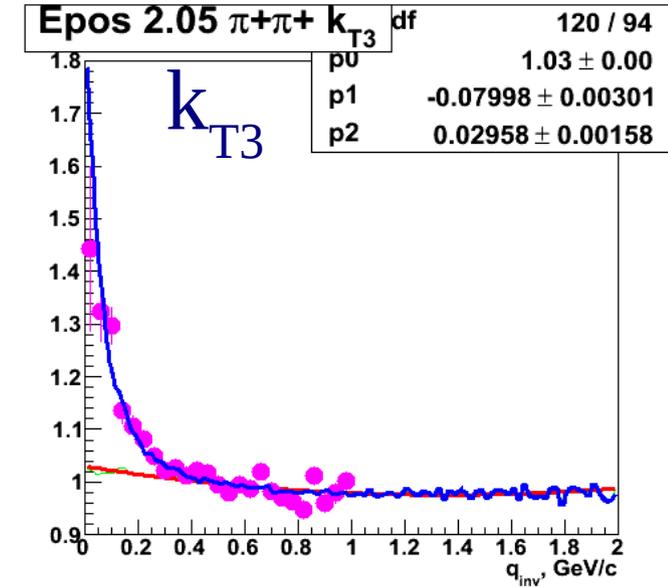
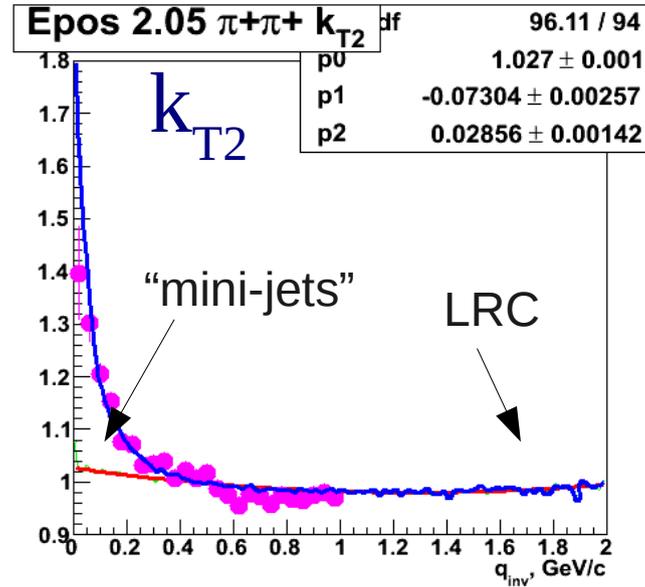
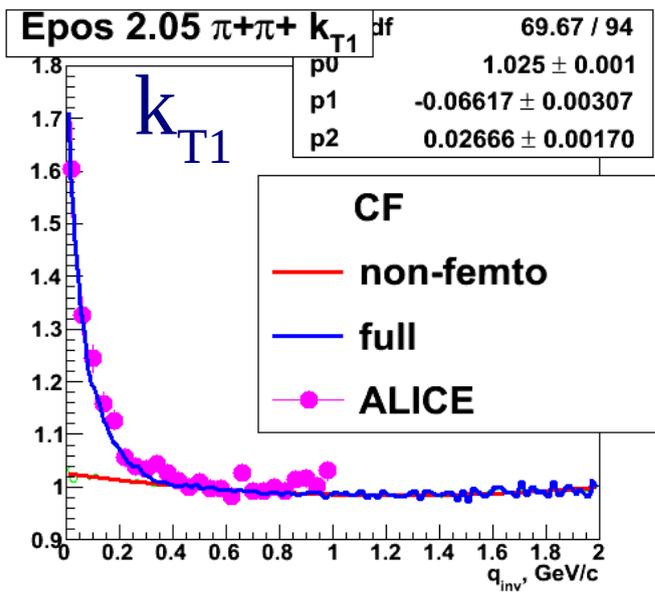
- Pure Epos correlation function (non-femto):

$$CF = [dN_{real}/dq_{inv}] / [dN_{mixed}/dq_{inv}]$$

# Epos non-femto: $a+bq_{inv}+cq_{inv}^2$



**Points** are ALICE  $\pi\pi$  correlation in  $pp\sqrt{s}=900\text{GeV}$  data [arXiv:1007.0516v1 hep-ex]  
**Blue curves** are the full scenario simulation with EPOS [arXiv:1010.0400v1 nucl-th]



# Epos: non-femto, pure, real/mix



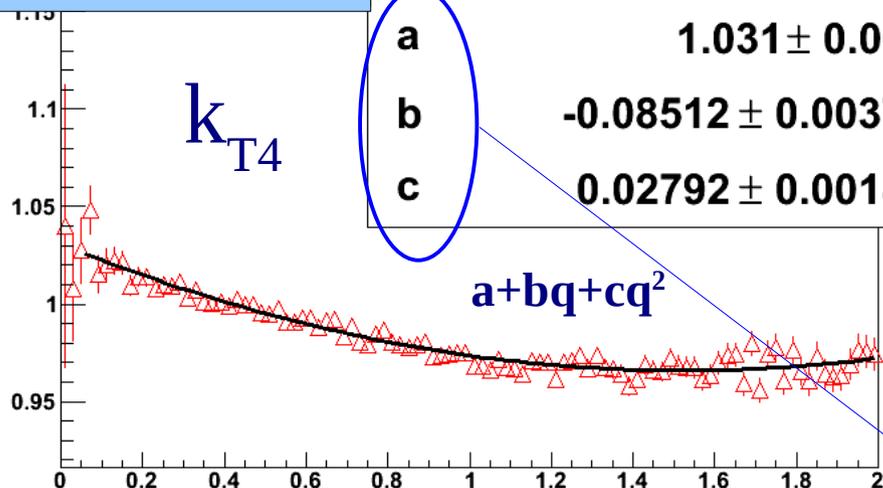
Non-femto

$\chi^2 / \text{ndf}$  89.17 / 94

**a**  $1.031 \pm 0.002$

**b**  $-0.08512 \pm 0.00377$

**c**  $0.02792 \pm 0.00189$

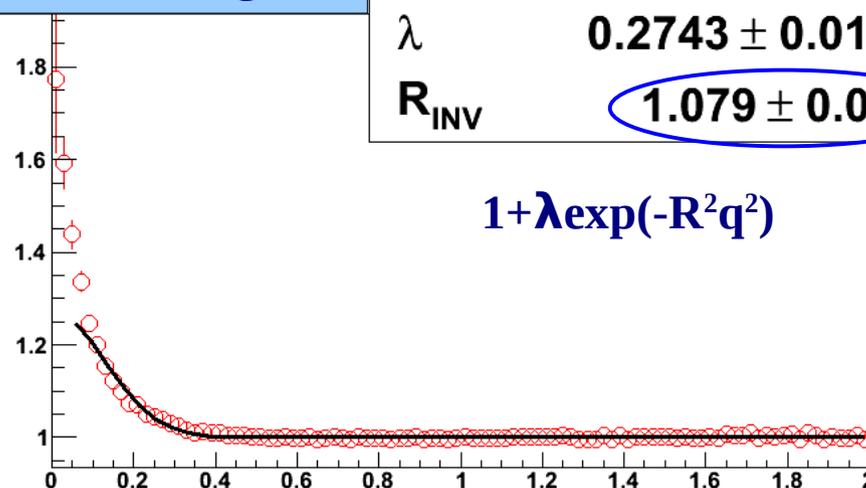


Pure Weight

$\chi^2 / \text{ndf}$  84.28 / 95

$\lambda$   $0.2743 \pm 0.0126$

$R_{\text{INV}}$   $1.079 \pm 0.027$



Full

$\chi^2 / \text{ndf}$  150.4 / 92

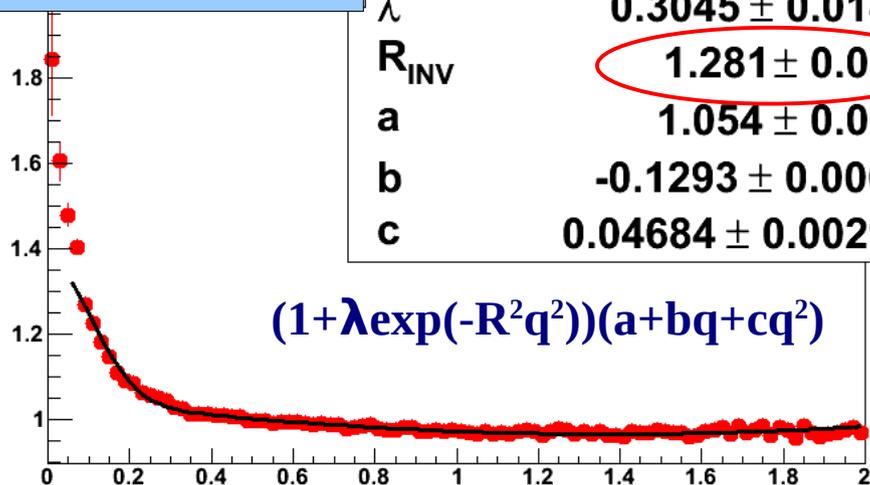
$\lambda$   $0.3045 \pm 0.0140$

$R_{\text{INV}}$   $1.281 \pm 0.038$

**a**  $1.054 \pm 0.003$

**b**  $-0.1293 \pm 0.0064$

**c**  $0.04684 \pm 0.00294$

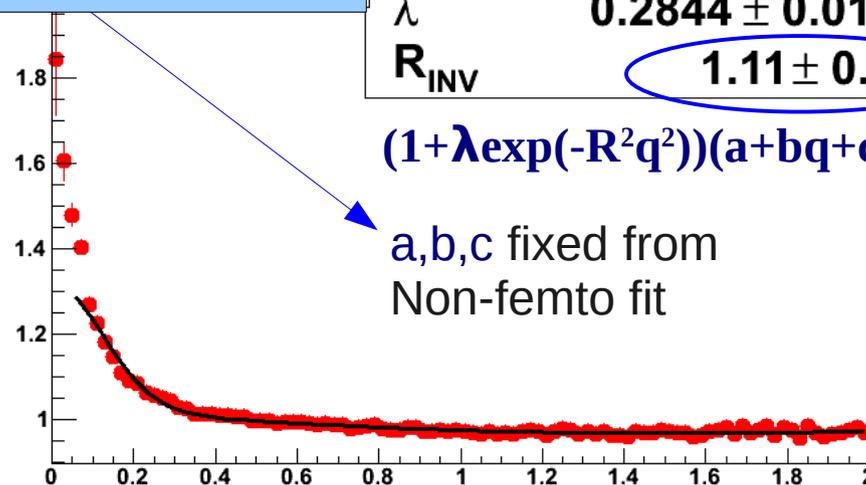


Full

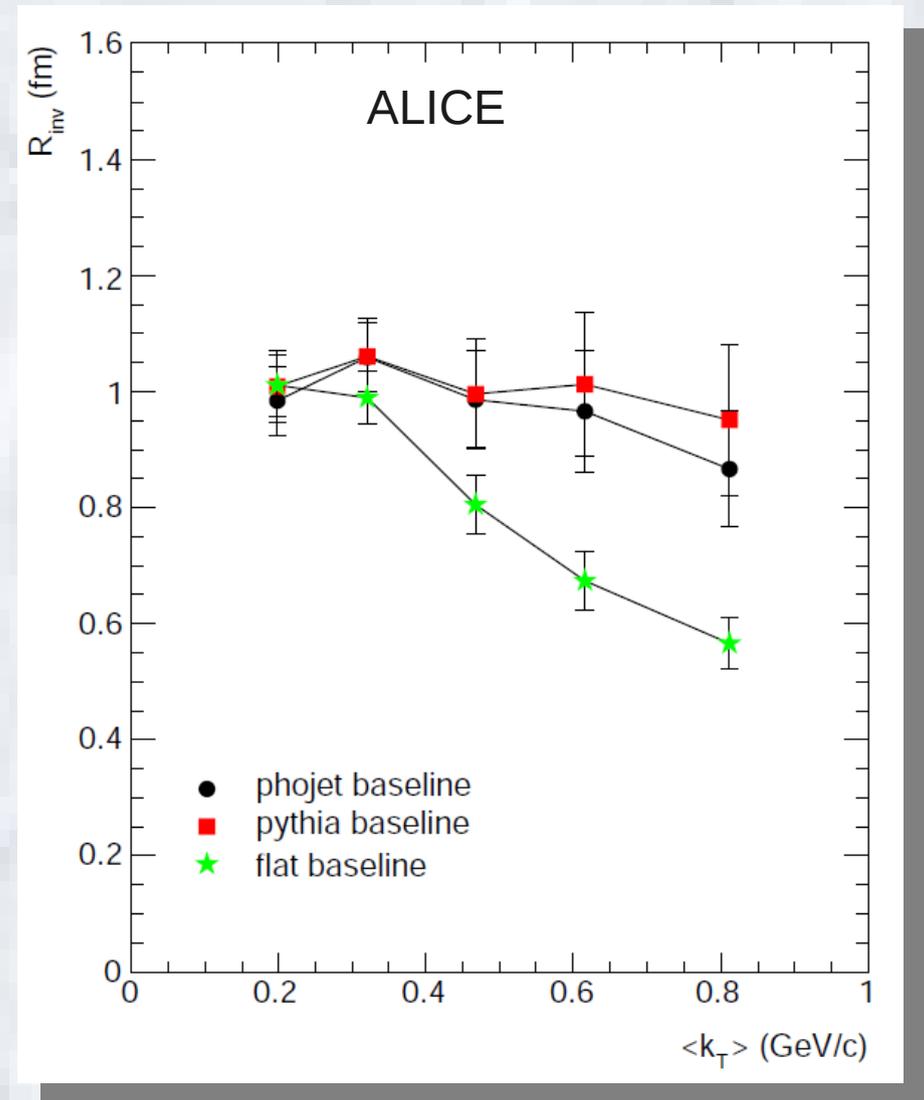
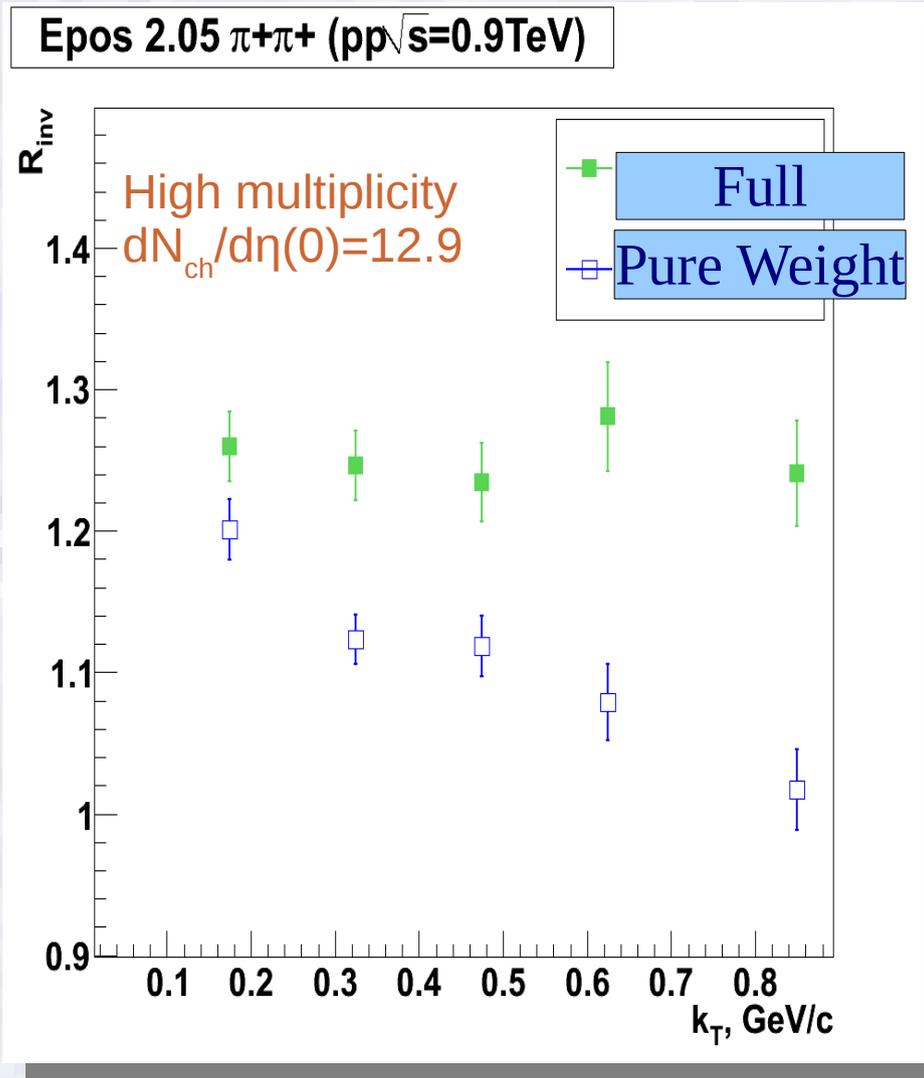
$\chi^2 / \text{ndf}$  200.3 / 95

$\lambda$   $0.2844 \pm 0.0112$

$R_{\text{INV}}$   $1.11 \pm 0.02$



# $R_{inv}$ pure and full



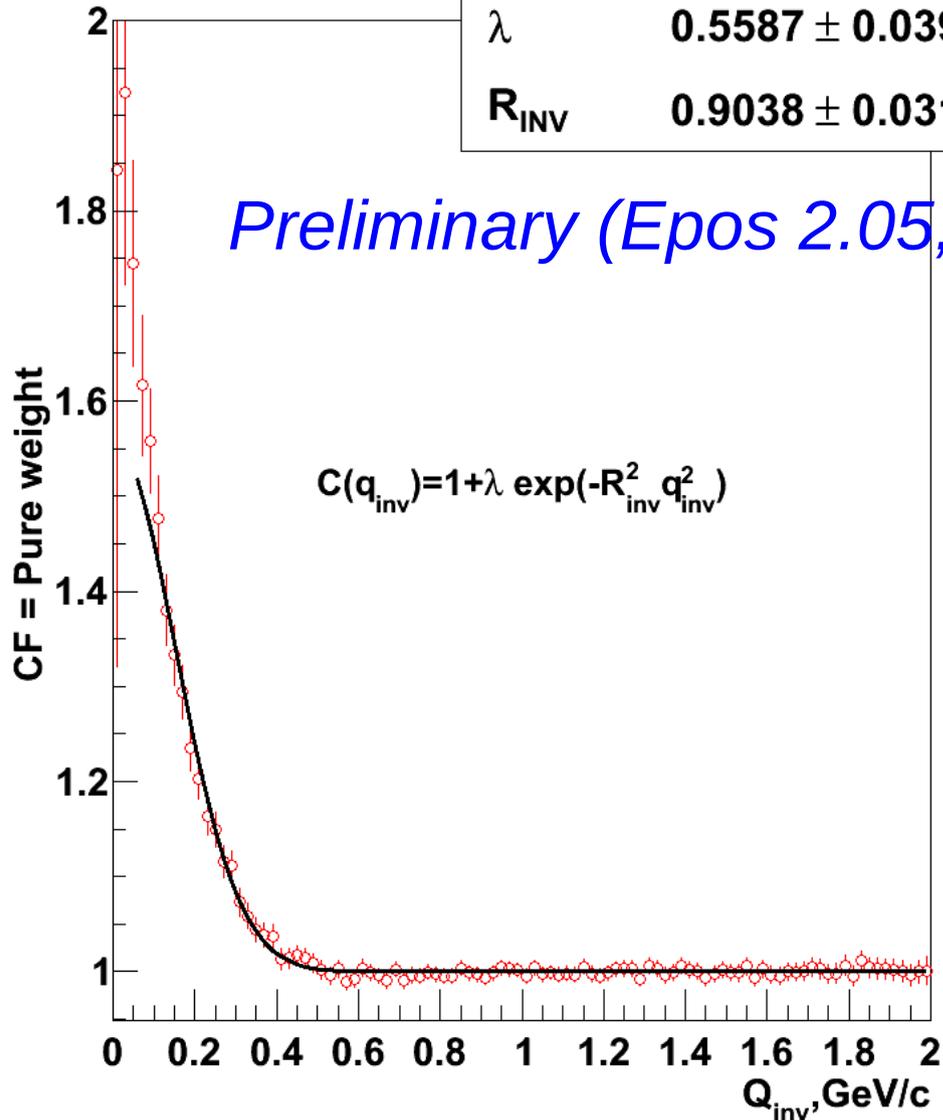
KK in Epos 2.05 (Preliminary)



# Epos 2.05 K+K+ pp $\sqrt{s}=900\text{GeV}$

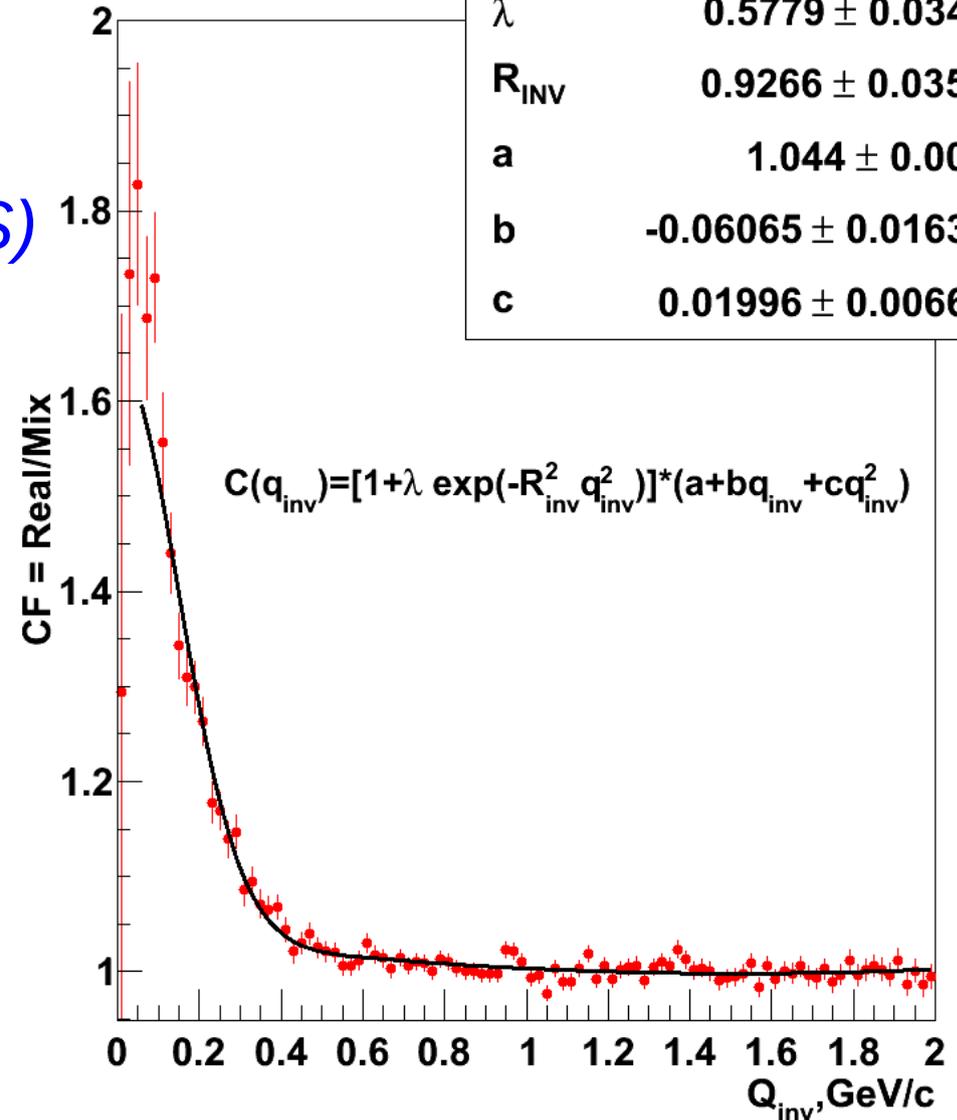
**Pure Weight**  $\chi^2 / \text{ndf}$  **19.53 / 95**

$\lambda$   **$0.5587 \pm 0.0390$**   
 $R_{\text{INV}}$   **$0.9038 \pm 0.0312$**



**Full**  $\chi^2 / \text{ndf}$  **105 / 92**

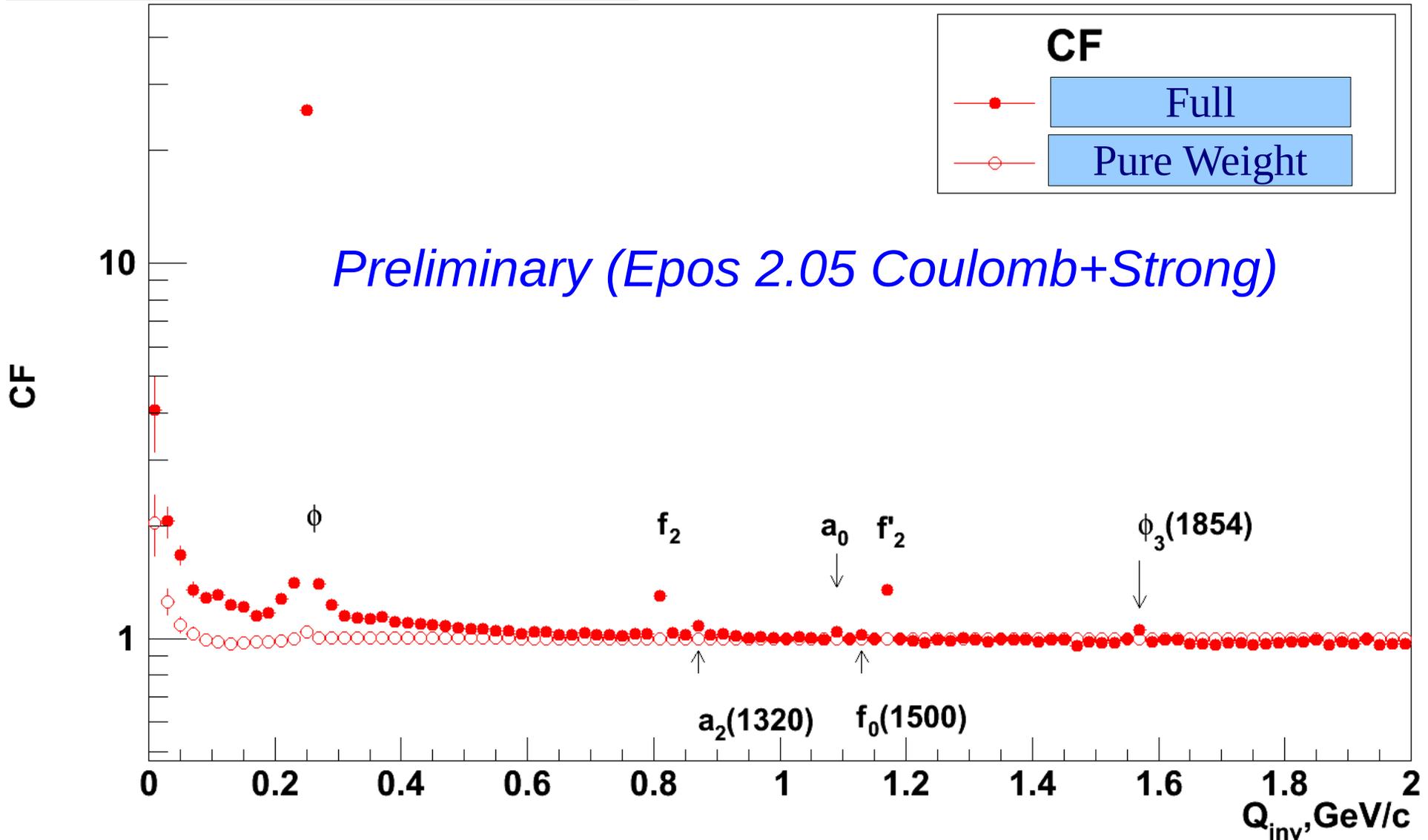
$\lambda$   **$0.5779 \pm 0.0349$**   
 $R_{\text{INV}}$   **$0.9266 \pm 0.0354$**   
**a**  **$1.044 \pm 0.009$**   
**b**  **$-0.06065 \pm 0.01639$**   
**c**  **$0.01996 \pm 0.00665$**





# Epos 2.05 K+K- pp $\sqrt{s}=900\text{GeV}$

**K<sup>+</sup>K<sup>-</sup> pp  $\sqrt{s}=900\text{GeV}$**



# Conclusion

1. The Epos Femto package **exists and works**
2. STAR HBT p-pi data was **described** with new Epos2+Femto
3. New studies (pp collisions at LHC energies) with Epos Femto are **in progress** [<http://arxiv.org/abs/1010.0400> ]
4. **Non-femtoscopic** effects could be very important in case of low multiplicity, e.g. pp collisions

*Thank you for your attention!*

# Extra Slides

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# Histograms



- Source function histograms:

$$\Delta R_{\text{out}}, \Delta R_{\text{side}}, \Delta R_{\text{long}} \text{ in LCMS}$$

- 1D correlation function histograms:

$$dN_{\text{real}}/dQ, \text{ projections: } dN_{\text{real}}/dQ_{\text{out}}, dN_{\text{real}}/dQ_{\text{side}}, dN_{\text{real}}/dQ_{\text{long}}$$

$$dN_{\text{mix}}/dQ, \text{ projections: } dN_{\text{mix}}/dQ_{\text{out}}, dN_{\text{mix}}/dQ_{\text{side}}, dN_{\text{mix}}/dQ_{\text{long}}$$

$$CF(Q), \text{ projections: } CF(Q_{\text{out}}), CF(Q_{\text{side}}), CF(Q_{\text{long}})$$

- 3D correlation function histograms:

$$d^3N_{\text{real}}/dQ_{\text{out}} dQ_{\text{side}} dQ_{\text{long}}$$

$$d^3N_{\text{mix}}/dQ_{\text{out}} dQ_{\text{side}} dQ_{\text{long}}$$

$$CF(Q_{\text{out}}, Q_{\text{side}}, Q_{\text{long}})$$

- A few technical histograms in addition

# Fit functions



- 1D fit function:

$$1 + \lambda \exp(-R_{inv}^2 Q_{inv}^2)$$

$$1 + \lambda_1 \exp(-R_1^2 Q_{inv}^2) + \lambda_2 \exp(-R_2^2 Q_{inv}^2)$$

$$(1 + \lambda \exp(-R_{inv}^2 Q_{inv}^2)) * (1 + \delta Q_{inv}^2)$$

$$(1 + \lambda \exp(-R_{inv}^2 Q_{inv}^2)) * (a + b Q_{inv} + c Q_{inv}^2)$$

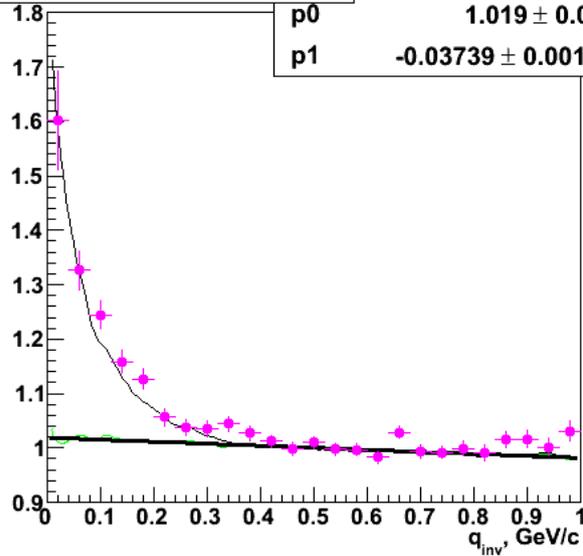
- 3D fit function:

$$1 + \lambda \exp(-R_{out}^2 Q_{out}^2 - R_{side}^2 Q_{side}^2 - R_{long}^2 Q_{long}^2)$$

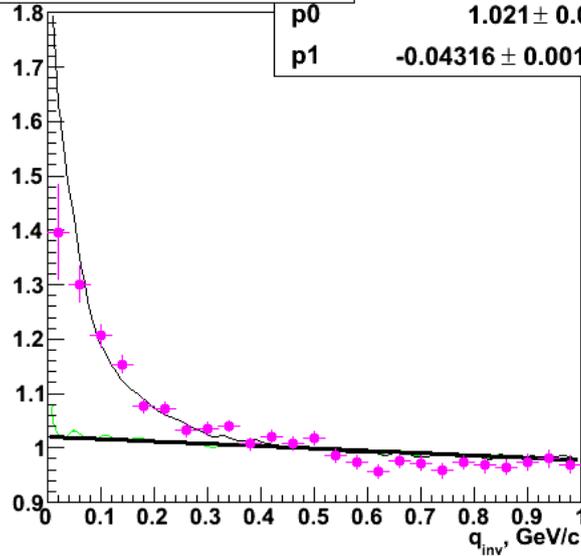
# $a+bq_{inv}$ in $\pi^+\pi^+$ CF



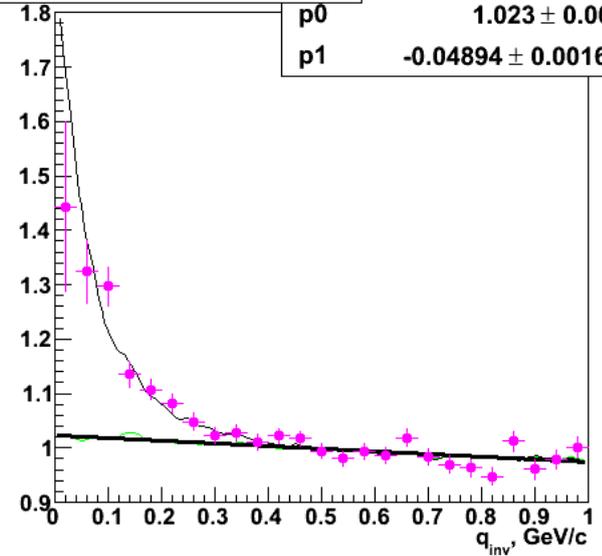
**Epos 2.05  $\pi^+\pi^+$   $k_{T1}$**  df 42.47 / 45  
 p0 1.019 ± 0.001  
 p1 -0.03739 ± 0.00157



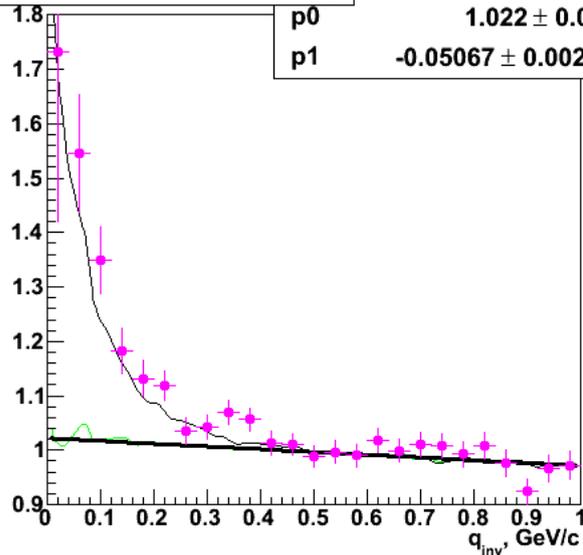
**Epos 2.05  $\pi^+\pi^+$   $k_{T2}$**  df 61.54 / 45  
 p0 1.021 ± 0.001  
 p1 -0.04316 ± 0.00136



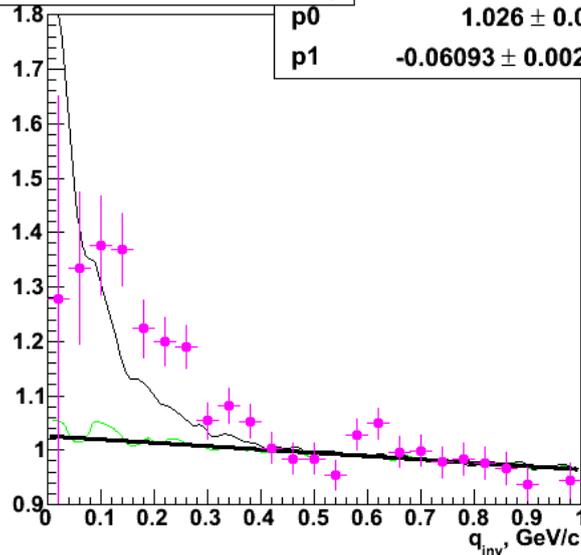
**Epos 2.05  $\pi^+\pi^+$   $k_{T3}$**  df 64.7 / 45  
 p0 1.023 ± 0.001  
 p1 -0.04894 ± 0.00165



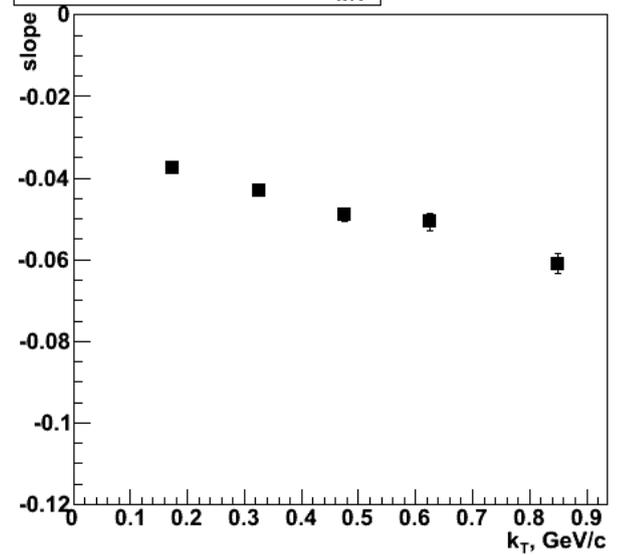
**Epos 2.05  $\pi^+\pi^+$   $k_{T4}$**  df 35.15 / 45  
 p0 1.022 ± 0.001  
 p1 -0.05067 ± 0.00216



**Epos 2.05  $\pi^+\pi^+$   $k_{T5}$**  df 63.55 / 45  
 p0 1.026 ± 0.002  
 p1 -0.06093 ± 0.00235



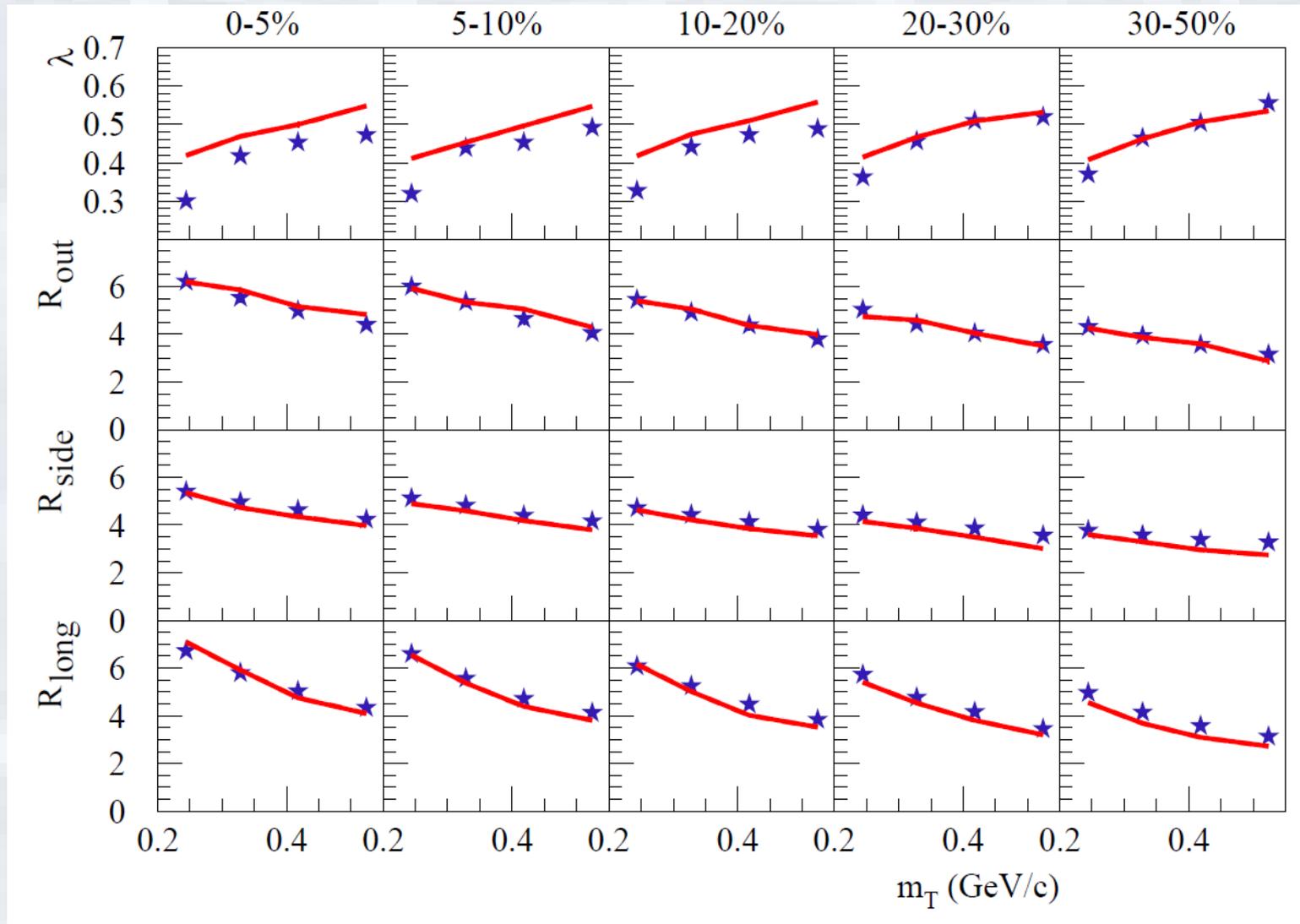
**Slope from fit= $a+bq_{inv}$**



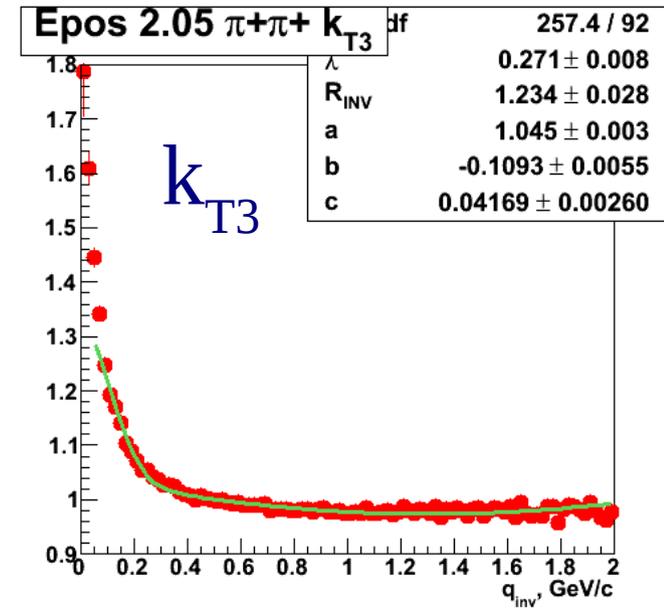
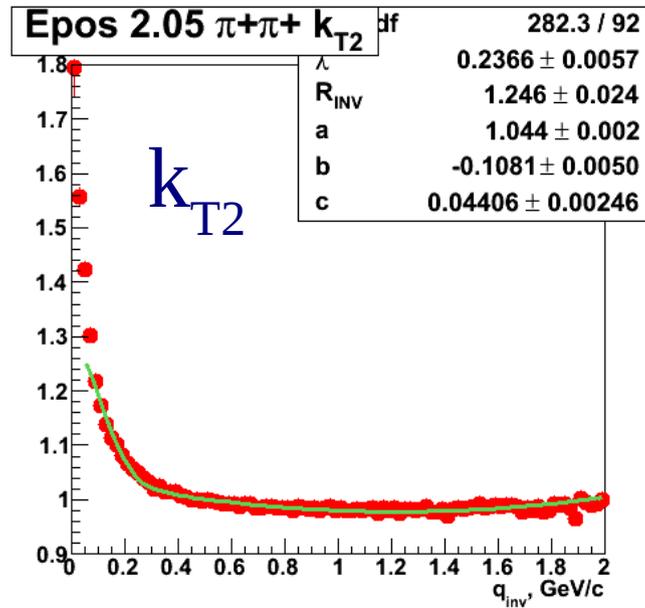
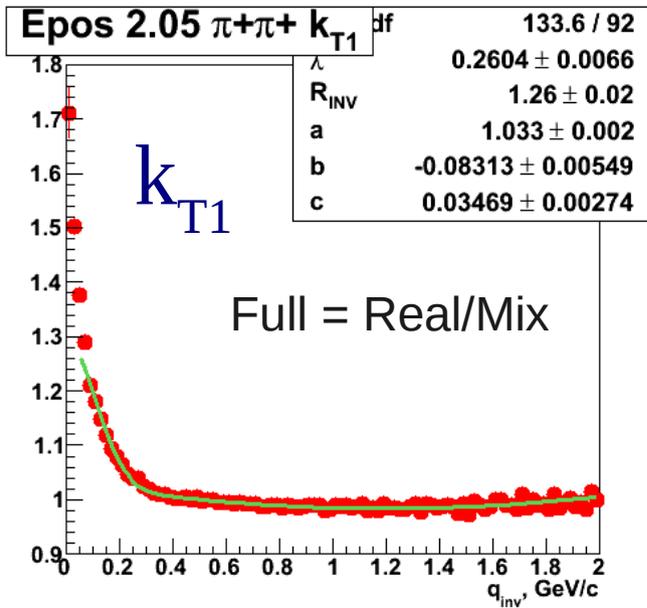


# Femtoscopic radii (full calculation)

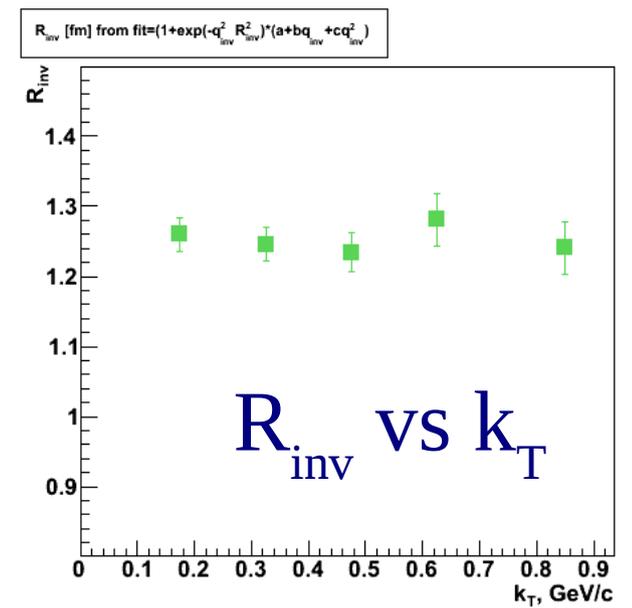
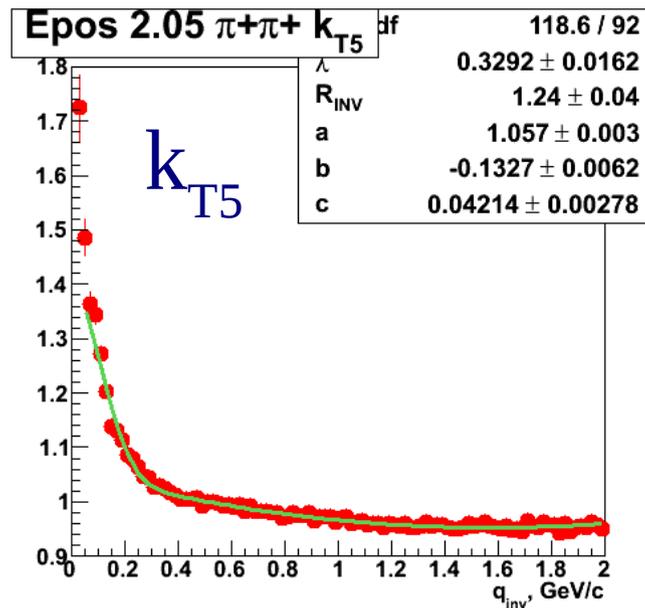
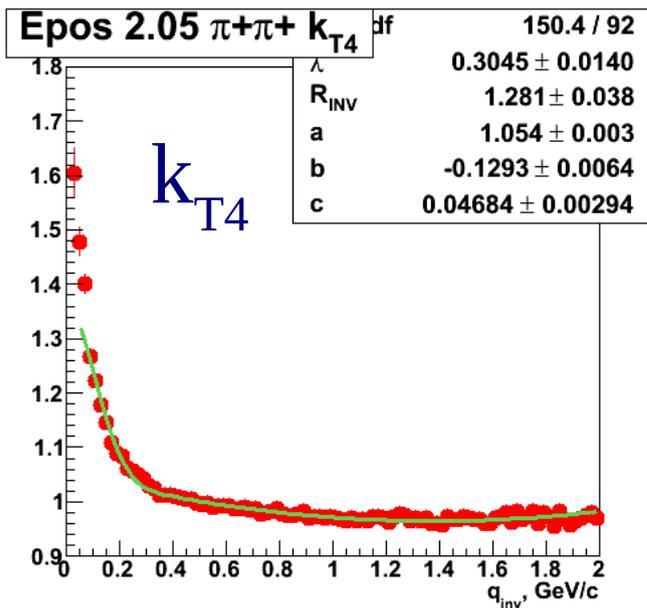
$R_{out}$ ,  $R_{side}$ , and  $R_{long}$  as a function of  $m_T$  for different centralities (0-5% most central, 5-10% most central, and so on). The full lines are the full calculations (including hadronic cascade), the stars data of STAR



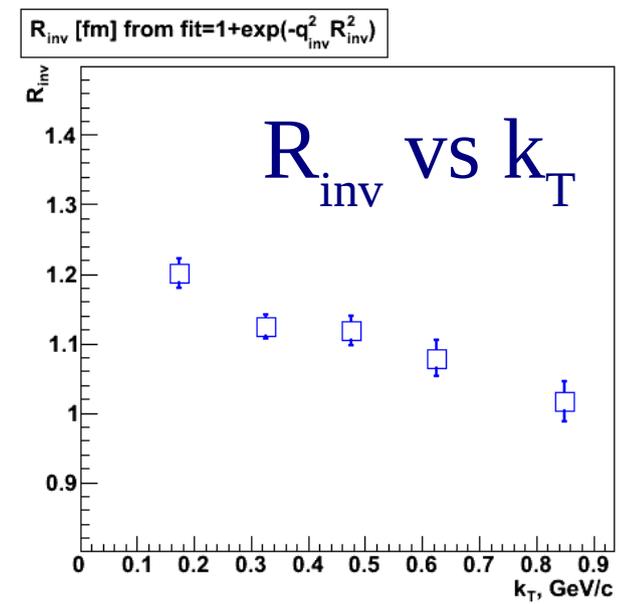
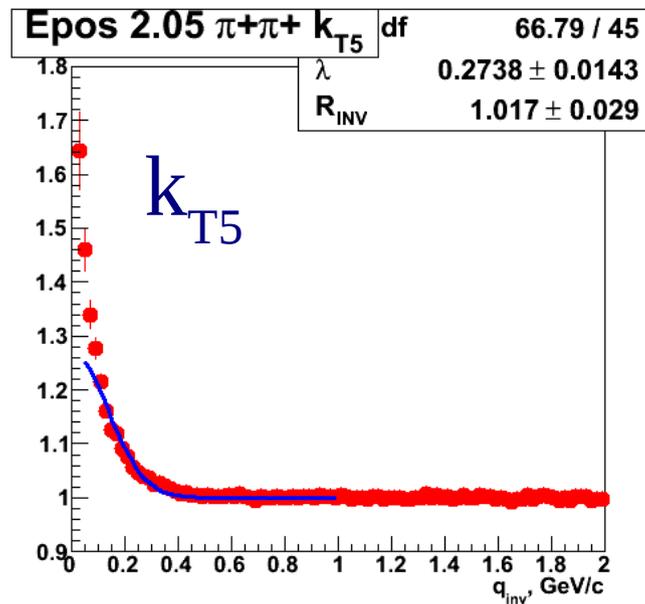
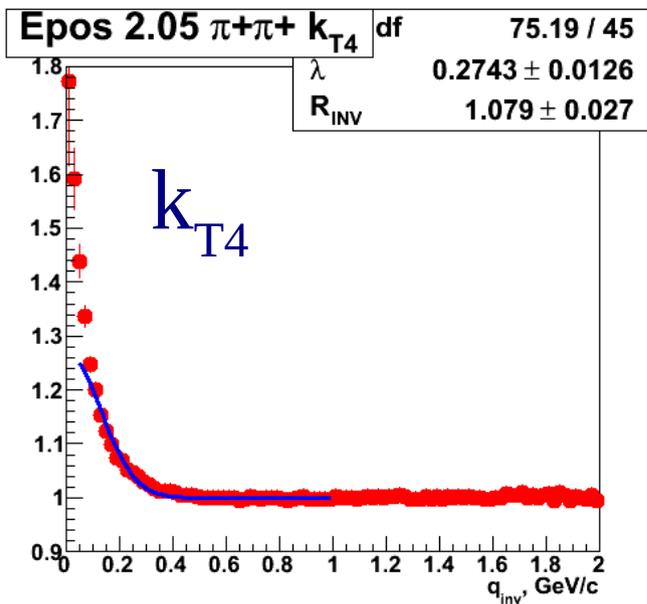
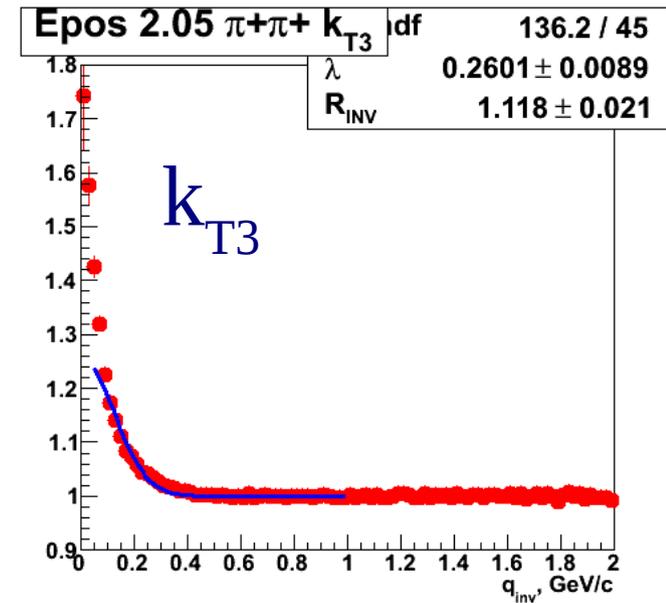
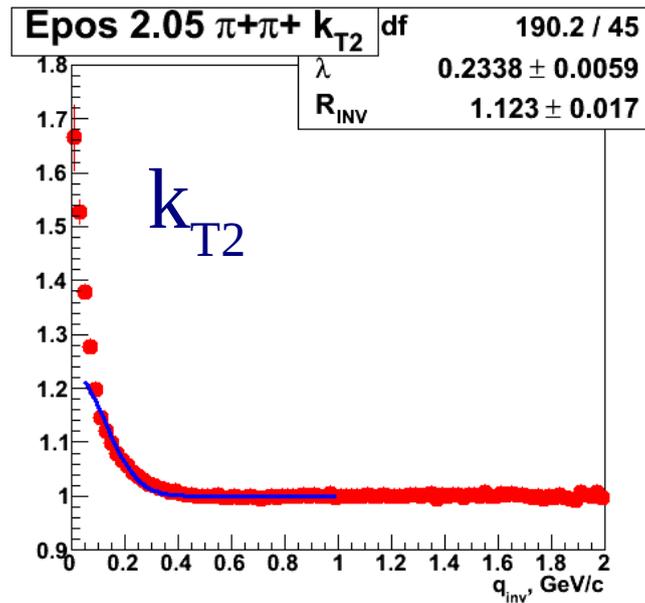
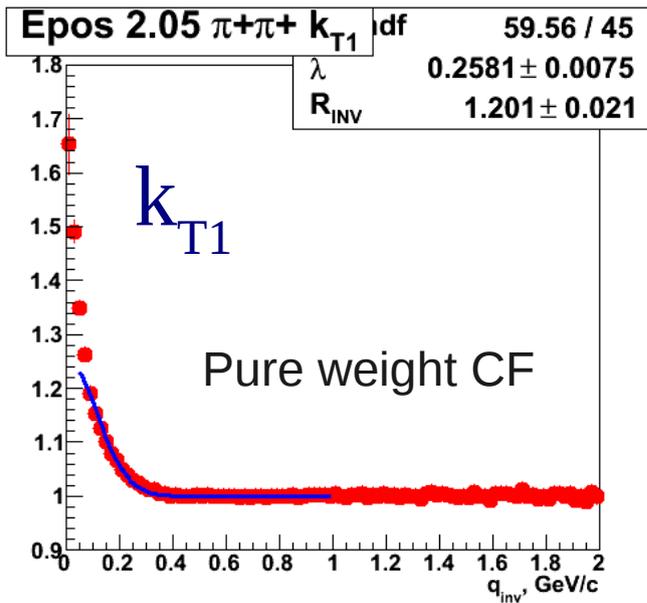
# Epos full: $(1 + \lambda \exp(-R^2 q^2))(a + bq + cq^2)$



PHYSICS OF ATOMIC NUCLEI Vol. 72 No. 4 2009



# Epos pure weight: $(1 + \lambda \exp(-R^2 q^2))$



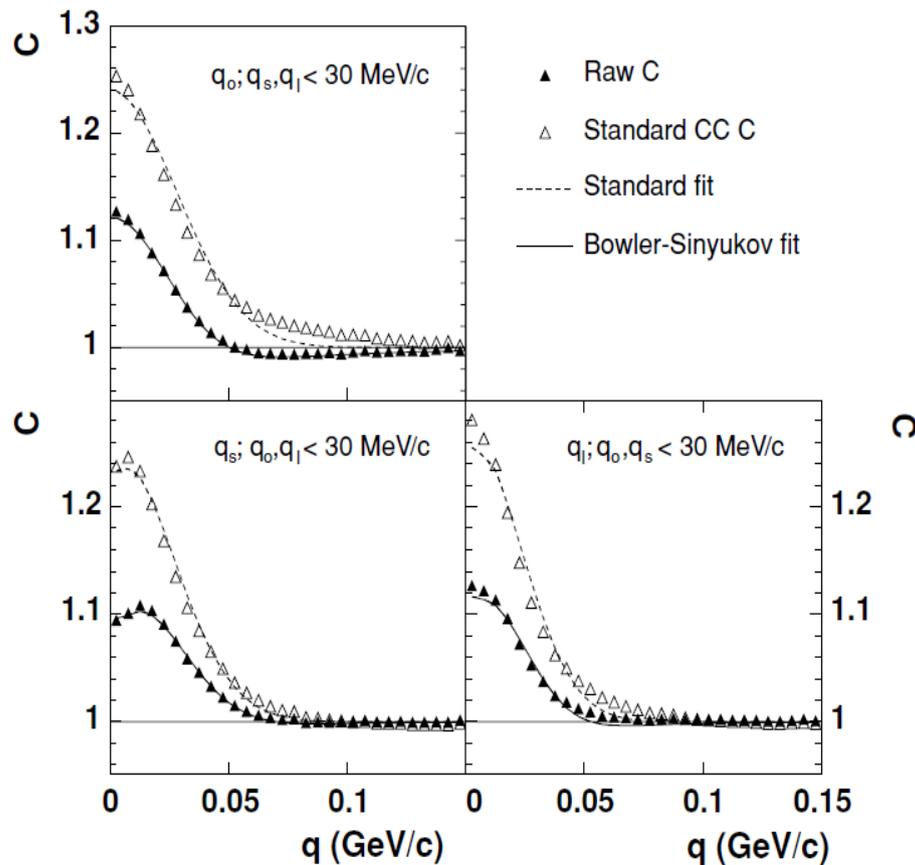
# STAR experimental results



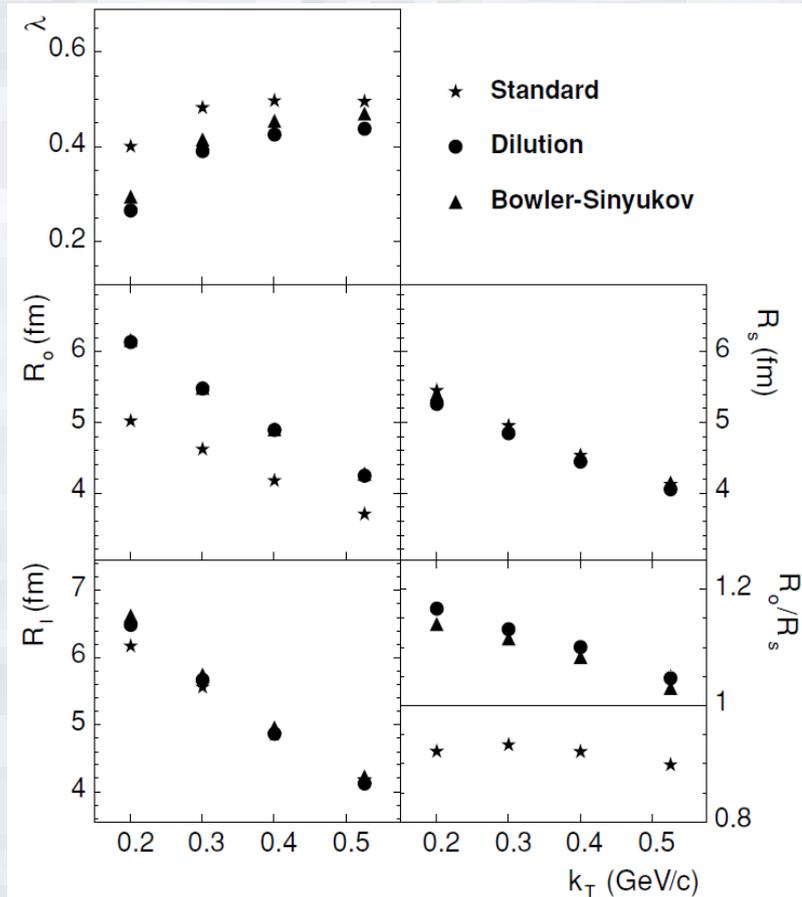
RHIC-STAR:  $\pi\pi$  femtoscopy for Au+Au  $\sqrt{s_{NN}}=200\text{GeV}$

[PHYSICAL REVIEW C 71, 044906 (2005)]

Projection of 3-d correlation function



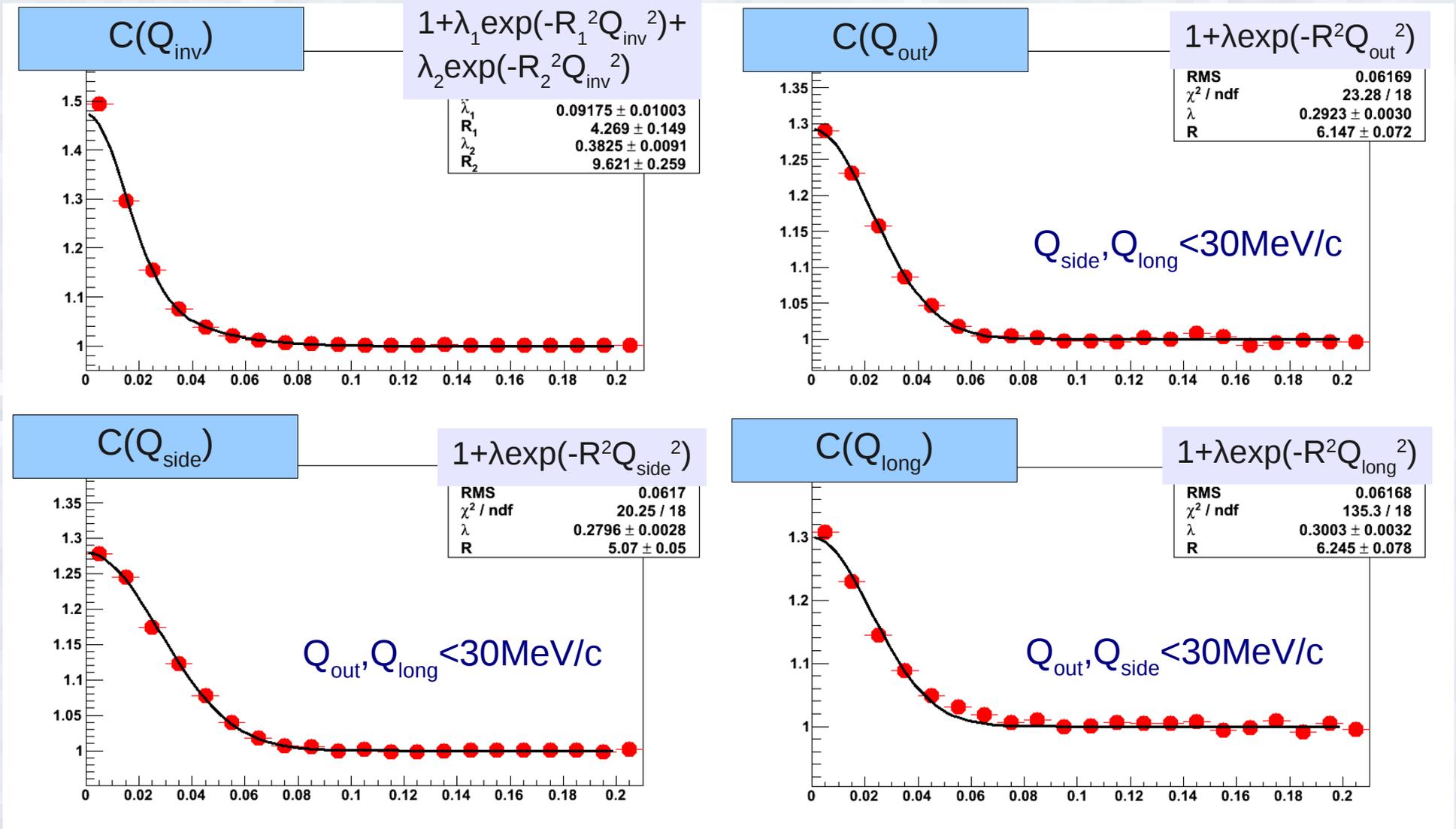
3-d fit results (3 variants of Coulomb)



# Femto package: 1d CF



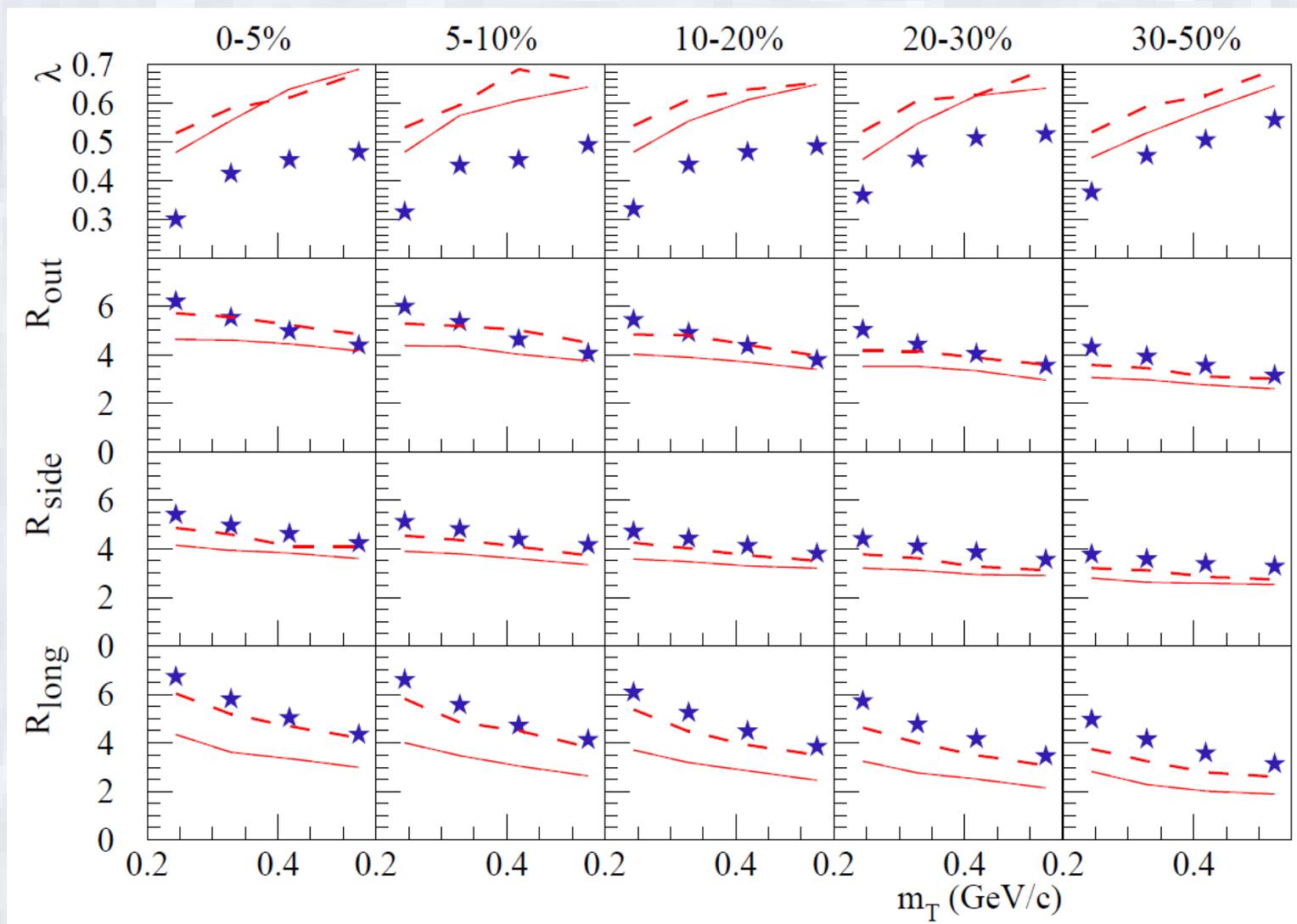
## Example of 1d pi+pi+ correlation function for central events



# Femtoscopic radii (other scenarios)



**Full line** the calculations are done without hadronic cascade (scenario 2).  
**Dashed lines** with a hydrodynamic evolution through the hadronic phase with freeze-out at 130 MeV (scenario 3).



# Flux tube

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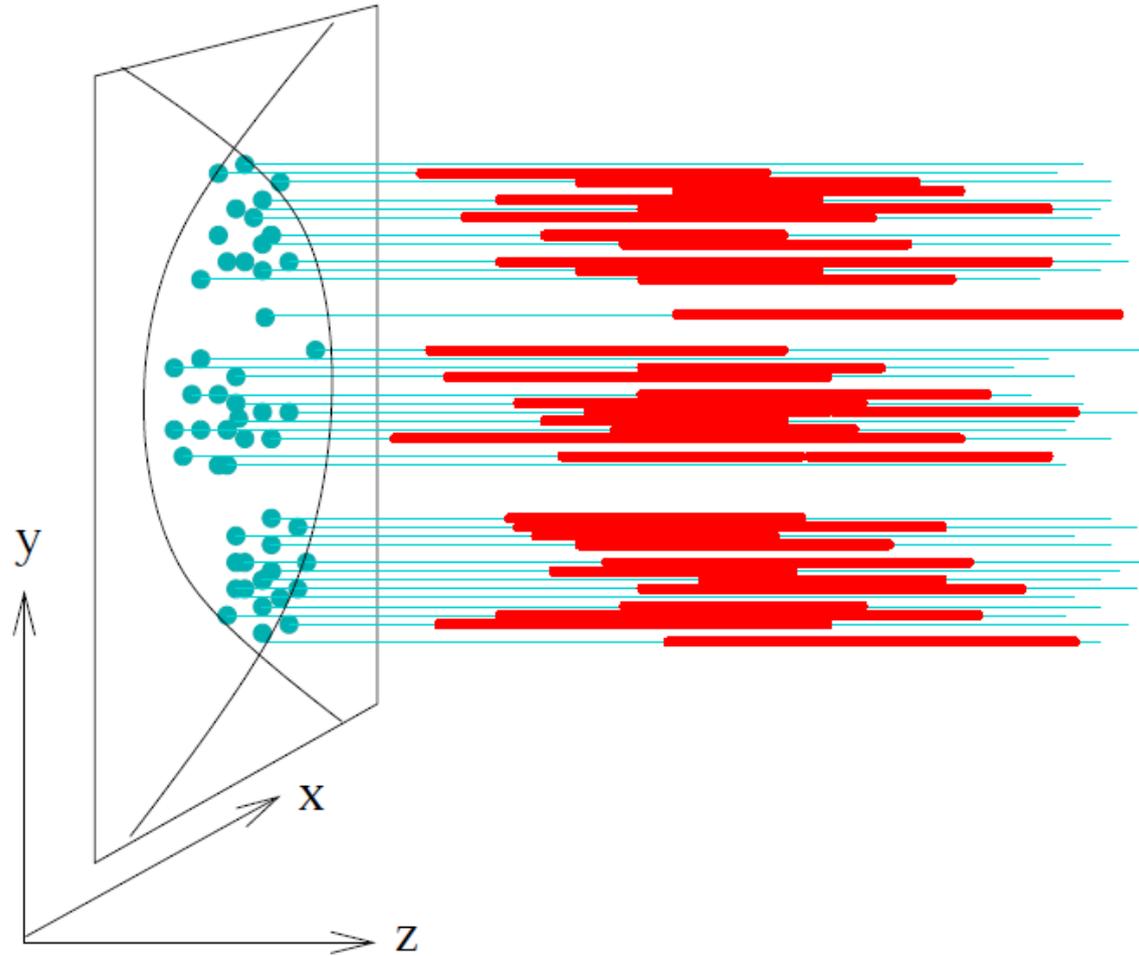


Figure 1: Macroscopic flux tubes (three in this example), made out of many individual ones, of variable length.

# 3+1 Hydro

Core evolves according to the equations of hydrodynamics:

local energy-momentum conservation

$$\partial_\mu T^{\mu\nu} = 0, \quad \nu = 0, \dots, 3,$$

and the conservation of net charges,

$$\partial N_k^\mu = 0, \quad k = B, S, Q,$$

with  $B$ ,  $S$ , and  $Q$  referring to respectively baryon number, strangeness, and electric charge.

Here: ideal hydrodynamics:

$$T^{\mu\nu} = (\epsilon + p) u^\mu u^\nu - p g^{\mu\nu}, \quad N_k^\mu = n_k u^\mu,$$

where  $u$  is the four-velocity of the local rest frame (unknowns:  $\epsilon(x)$ ,  $u(x)$ ,  $n_k(x)$ ).

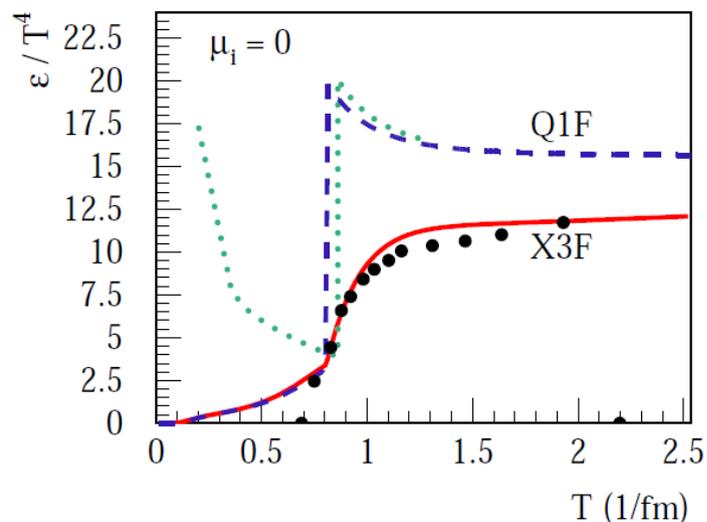


Figure 11: Energy density versus temperature, for our equation-of-state X3F (full line), compared to lattice data [66] (points), and some other EoS choices, see text.

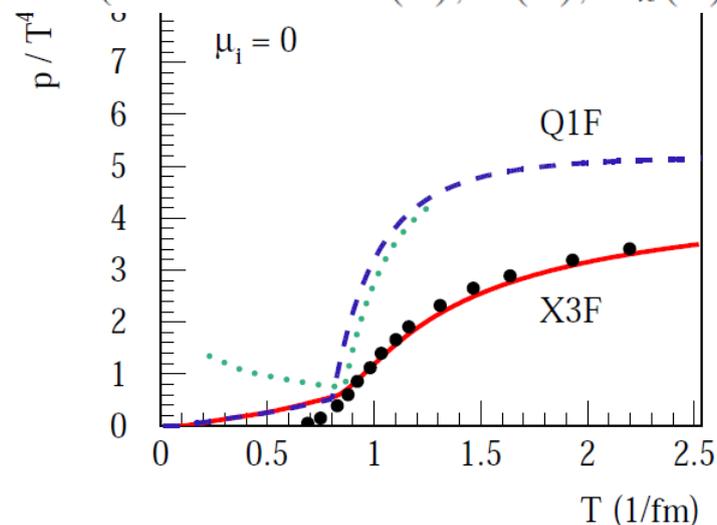
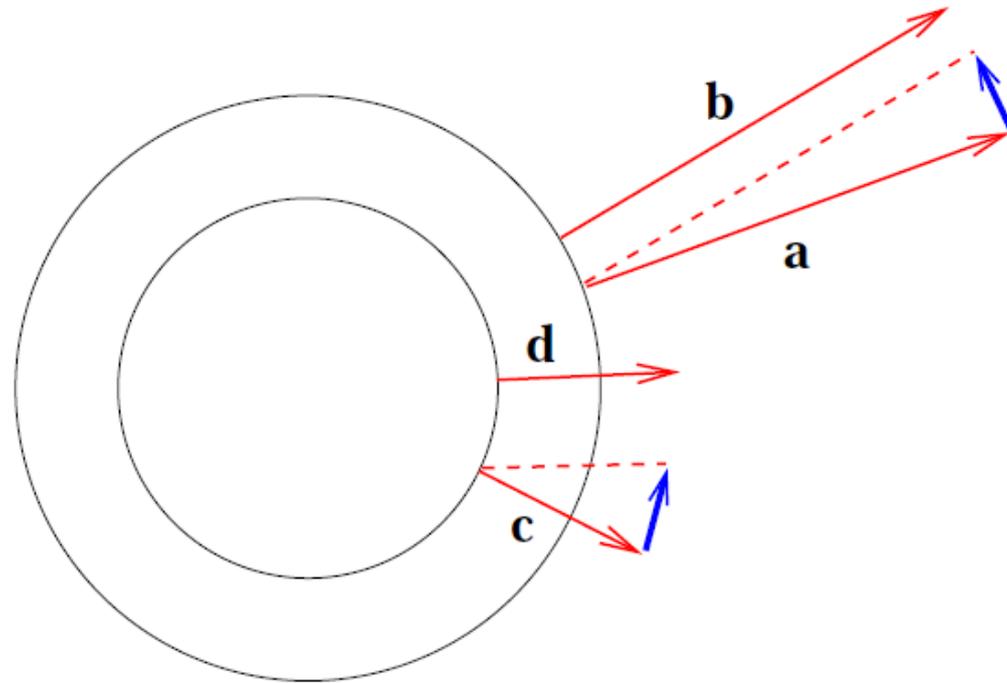


Figure 12: Pressure versus temperature, for our equation-of-state X3F (full line), compared to lattice data [66] (points), and some other EoS choices, see text.

Radial flow effect on  $m_T$  dependence of femtoscopic radii:



distances get smaller outwards for fixed momentum differences

# Basics of EPOS(parton model)

*Klaus Werner. Nucl.Phys.175-176(2008)81-87*

EPOS is a sophisticated multiple scattering approach based on partons and Pomerons (parton ladders), with special emphasis on high parton densities. The latter aspect, particularly important in proton-nucleus or nucleus-nucleus collisions, is taken care of via an effective treatment of Pomeron-Pomeron interactions, referred to as parton ladder splitting. In addition, collective effects are introduced after separating the high density central core from the peripheral corona. EPOS is the successor of the NEXUS model.

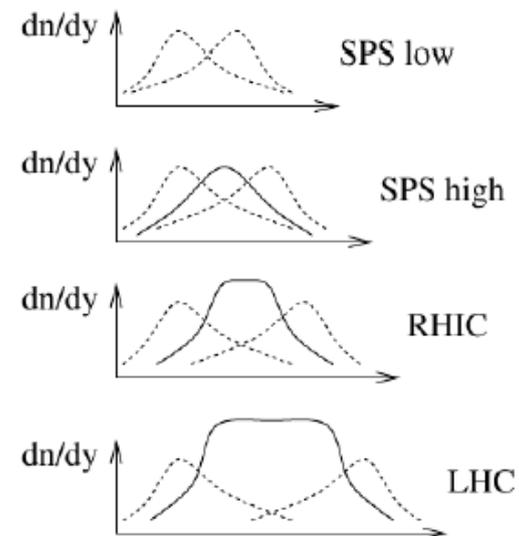
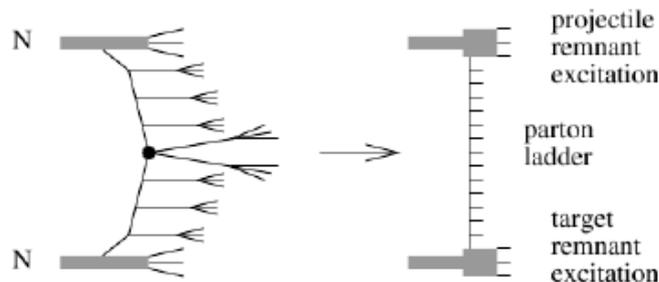
**E**nergy conserving quantum mechanical multiple scattering

approach based on

**P**arton (parton ladders)

**O**ff-shell remnants, and

**S**plitting of parton ladders



## 4 Tests

### Check basic “soft physics” RHIC data (only AuAu $\geq 200$ distributions)

#### – Particle yields and eta distributions

- \* STAR and PHENIX  
average yields and mean pt of pions, kaons, protons, lambdas, xis vs centrality
- \* BRAHMS  
eta distr for different centralities 0-5% 5-10% 10-20% 20-30% 30-40% 40-50%  
rapidity distr of pions, kaons, protons(central)  
mean pt vs rapidity of pions, kaons (central)

#### – pt spectra

- \* PHOBOS: pt distributions of charged particles at centralities 0-6%, 6-15%, ..., 45-50%
- \* BRAHMS: pt distributions of pions, kaons, protons at given rapidity (central)
- \* PHENIX: pt distributions of pions, kaons, protons for different centralities:  
0-5%, 5-10%, 10-20%, 20-30%, 30-40%, 40-50%, 50-60%, 60-70%, 70-80%, 80-92%
- \* STAR: mt distributions of pions, kaons, protons for different centralities  
0-5%, 5-10%, 10-20%, 20-30%, 30-40%, 40-50%, 50-60%, 60-70%, 70-80 %
- \* STAR pt distributions of strange baryons for different centralities:  
0-5%, 10-20%, 20-40%, 40-60%, 60-80%

#### – $v_2$ :

- \* PHOBOS:  $v_2$  vs eta for different centralities: MB, 3-15, 15-25, 25-50, 0-40  
 $v_2$  vs centrality  $v_2$  vs pt of charged particles, 0-50
- \* STAR  $v_2$  vs pt of  $\pi$ , K, prt for different centralities  
MB, 0-5, 20-30, 40-50;  $\Lambda$  and  $K_s$  10-40, 40-80
- \* PHENIX  $v_2$  vs pt of  $\pi$ ,  $K$ ,  $p$  for 0-60, 20-60